

**DEALING WITH DATA-POOR FISHERIES: A CASE  
STUDY OF THE BIG SKATE (*RAJA BINOCULATA*) IN  
BRITISH COLUMBIA'S GROUND FISH FISHERY**

by

Sabrina Garcia  
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# APPROVAL

**Name:** Sabrina Garcia  
**Degree:** Master of Resource Management  
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**Title of Thesis:** Dealing with data-poor fisheries: A case study of the big skate (*Raja binoculata*) in British Columbia's groundfish fishery

**Examining Committee:**

**Chair:** Jenna Bedore  
Master of Resource Management Student, School of Resource and Environmental Management, Simon Fraser University

---

**Dr. Andrew B. Cooper**  
Senior Supervisor  
Associate Professor, School of Resource and Environmental Management, Simon Fraser University

---

**Dr. Nicholas K. Dulvy**  
Committee Member  
Professor, Canada Research Chair in Marine Biodiversity and Conservation, Department of Biological Science, Simon Fraser University

---

**Dr. Jaquelynn R. King**  
Committee Member  
Research Scientist, Pacific Biological Station, Fisheries and Oceans Canada (DFO)

**Date Defended/Approved:** \_\_\_\_\_

## ABSTRACT

Groundfish fisheries target big skate (*Raja binoculata*) off the British Columbia coast. Catch comes mainly from Queen Charlotte Sound (QCS) and North Hecate Strait (NHS). Until now, sufficient data to evaluate stock status was not available. I parameterized a Graham-Schaefer model using catch (1996-2010), catch-per-unit-effort (1996-2010), and fishery-independent surveys (1984-2009) to estimate current abundance. QCS and NHS appear stable at their median estimated carrying capacities of 698,000 and 501,000 tonnes. Maximum sustainable yield (MSY) equalled 21,800 and 16,200 tonnes for QCS and NHS. Depletion-corrected average catch (DCAC) potential yield, a conservative estimate of MSY, equalled 17,500 and 13,000 tonnes for QCS and NHS. DCAC sustainable yield, total removals that may likely maintain a stock at current abundance, equalled 370 and 330 tonnes for QCS and NHS. To maintain current abundance, managers should monitor catches and keep them similar to historic catches since they do not appear to affect population dynamics.

**Keywords:** Stock assessment; elasmobranchs; population dynamics; Bayesian; life history

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# 1: INTRODUCTION

Fishery stock assessments serve as the backbone of effective fisheries management by allowing scientists to make population predictions under a variety of management scenarios. However, providing management advice for fish stocks is problematic even for data-rich fisheries (Walters and Maguire, 1996). For example, stock assessment models may have difficulty fitting to contrasting abundance trends resulting in population estimates with high uncertainty. In cases where data are unavailable or uninformative, even the best stock assessment models will be unable to provide managers with information that is necessary for effective management.

Fishery managers need to account for uncertainty that is present in data to make effective management decisions. Uncertainty in data for fish stocks arises from multiple sources such as incomplete fishery catch and effort data, from abundance indices that may not capture true population trends, or from observation error during data collection. Fisheries and Oceans Canada (DFO) adopted the precautionary approach which requires them to account for uncertainty when making management decisions to avoid harm to stocks or the ecosystem (DFO, 2006). DFO's adherence to the precautionary approach is one aspect of its larger Sustainable Fisheries Framework, which requires assessment on a stock-by-stock basis to ensure the sustainable use and conservation of Canadian fisheries (DFO, 2009). As part of this Sustainable Fisheries

Framework, Canada has implemented a National Plan of Action for Sharks (NPOA-Sharks) as recommended by the United Nations Food and Agricultural Organization (FAO, 1999). Under the NPOA-Sharks, Canada plans to assess sharks (all sharks, skates, and chimaeras) and update the FAO every four years on stock status and resultant changes to management practices (DFO, 2007). The NPOA-Sharks aims to take a precautionary approach to management because sharks may be relatively more prone to over-fishing than bony fish due to their life history traits, such as late age of maturity and longevity (Hoenig and Gruber, 1990; Dulvy and Forrest, 2010).

Although elasmobranchs (sharks, skates, and rays) are targeted in fisheries and caught as valued bycatch worldwide, fishery scientists consistently have difficulty assessing them due to the lack of species-specific identification, short time series of catch data, and uncertainties in life history data. Elasmobranch fisheries are generally data-limited due to a lack of resources to record species-specific catch data (catch equals landings plus discards). Only 30% of retained shark landings reported to the FAO are recorded by species; the remainder are placed in generic categories (FAO, 2012). Additionally, minimal recording of discarded elasmobranch species leads to missing information on total catch, further complicating stock assessments (Bonfil, 1994). Another common problem faced by fishery scientists assessing elasmobranch stocks is the length of the catch time series relative to generation time. For example, although tuna longline fisheries in the North Atlantic have been ongoing since the 1960's, species-specific shark catch data are only available post-1994 (Clarke,

2008). For porbeagle and short-fin mako sharks (*Lamna nasus* and *Isurus oxyrinchus*, respectively) caught in these tuna longline fisheries, 20 years of data may not be sufficient for reliable stock assessments considering these species live to be 32 and 24 years old, respectively (Dulvy et al, 2008). Finally, data limitations also arise in elasmobranch life history traits (i.e., static measures of an organism's life cycle) because of difficulties in estimating litter size, breeding interval, and age.

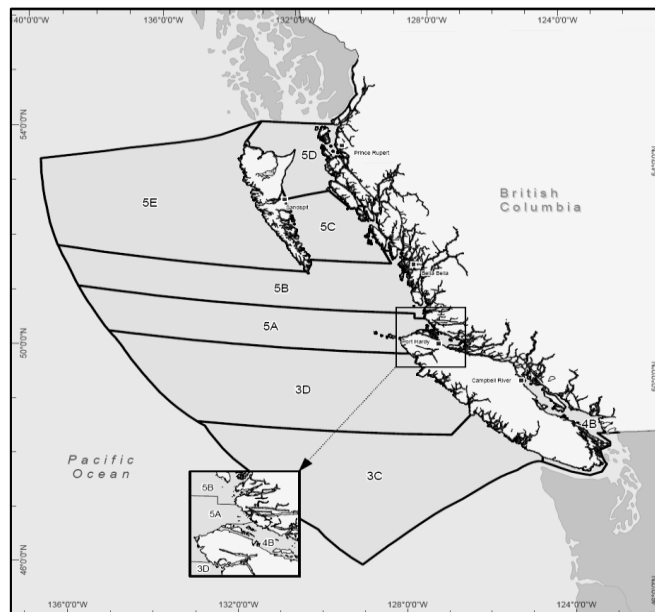
Fishery scientists use a variety of methods to assess data-limited fisheries depending on the data available and the uncertainty present in those data. Life history traits, such as natural mortality and life span, can provide insight to the ability of a stock to withstand different levels of exploitation (Hoenig and Gruber, 1990; Beddington and Kirkwood, 2005; Dulvy and Forrest, 2010). Fishery scientists can use Bayesian statistics to combine information known before data are collected (e.g., from previous research or expert opinion) with information contained in the observed data (McAllister and Kirkwood, 1998). Prior information is included in models via probability distributions around a range of parameter values. The shape of the probability distribution determines the belief associated with each parameter value. For example, a uniform distribution assumes all parameter values within a specified range are equally probable. Prior knowledge may help models fit to data, especially when dealing with data-limited stocks.

Depletion-corrected average catch analysis (DCAC) is another method used by fishery scientists to assess data-limited stocks which incorporates uncertainty and requires relatively little data. DCAC accounts for a one-time

unsustainable reduction in stock size from its unfished biomass known as the “windfall” (MacCall, 2009). DCAC calculates an average catch that accounts for the “windfall” to estimate a sustainable yield. The sustainable yield is likely to be sustainable if stock abundance is at or near the levels of abundance experienced over the catch time series (i.e., not severely depleted) (MacCall, 2009). DCAC requires a time series of catch, an estimate of natural mortality ( $M$ ), the ratio of  $M$  to the fishing mortality that produces the maximum sustainable yield ( $F_{MSY}$ ), and an estimate of the depletion of the stock from the first to last year of the catch time series (MacCall, 2009). DCAC incorporates uncertainty by using probability distributions over a range of plausible parameter values in lieu of point estimates (Berkson et al., 2011), and thus is useful for setting catch targets.

DFO collects data on big skate (*Raja binoculata*) captured through groundfish fisheries in British Columbia (BC) to use for assessment and management. Big skate have been targeted in both the trawl and longline sectors of the groundfish fisheries in North Hecate Strait (NHS) and Queen Charlotte Sound (QCS) since 1996 (Figure 1). Onboard observers monitor all tows on all vessels trawling for groundfish in BC and record species composition of landings and discards, trawl tow time, fishing depth, and area fished since 1996. Since 2006, electronic monitoring systems record catch and discards in order to validate logbook data from the longline sector of the groundfish fishery. Additionally, weight and identification of all landed fish from all fishery sectors are validated through a dockside monitoring program. DFO also runs multiple fishery-

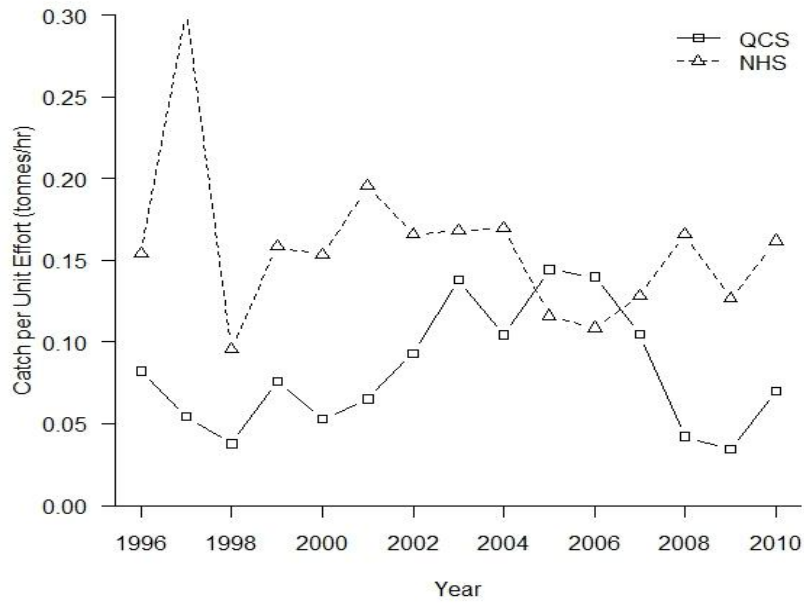
independent research surveys that encounter big skate and may provide indices of abundance along with length-at-age data (McFarlane and King, 2006).



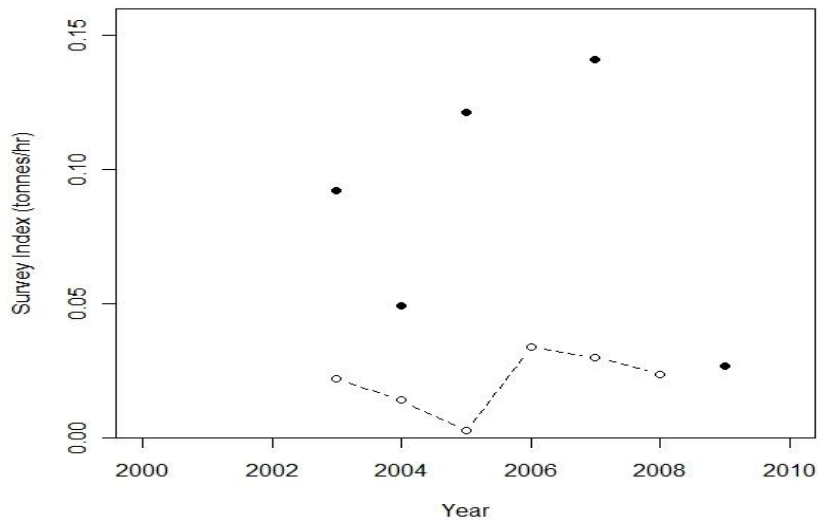
**Figure 1.** A map of the DFO statistical areas for the groundfish fishery. Areas 5A and 5B correspond to Queen Charlotte Sound and areas 5C and 5D correspond to North Hecate Strait.

The big skate fishery in QCS and NHS may be examples of data-limited fisheries despite the aforementioned available data. The fishery-dependent catch-per-unit-effort (CPUE) and research surveys indices have high variability and do not show strong contrast over the available time period, 1996-2010 (Figures 2-4). This lack of contrast in CPUE and research surveys may cause difficulty in parameter estimation for stock assessments (Hilborn and Walters, 1992). Difficulties in parameter estimation arise because models require variation in stock size and fishing effort to reliably estimate parameters (Hilborn and Walters, 1992). Additionally, the 15-year-long time series is short relative to the generation time of big skate: the age of maturity for big skate is approximately 6

years for males, and 8 years for females, with the oldest big skate in BC recorded at 26 years old (McFarlane and King, 2006).

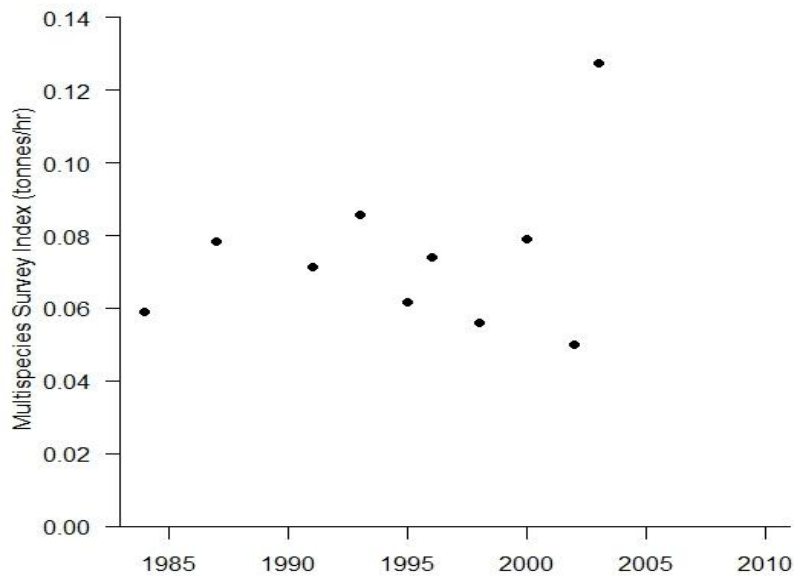


**Figure 2.** Trawl CPUE (tonnes/hr) for the groundfish fishery in Queen Charlotte Sound (QCS) and North Hecate Strait (NHS).



**Figure 3.** Survey indices of abundance for the 2003-2008 QCS Shrimp Survey (dashed line) and the QCS Synoptic Survey (black points) from 2003-2005, 2007, and 2009.





**Figure 4.** Survey index of abundance (tonnes/hr) for the Hecate Strait Multispecies Survey.

Limited migratory exchange occurs between big skate stocks in QCS and NHS, and therefore separate assessments and management plans are required for each area (King and McFarlane, 2010). I assessed each stock separately using two methods: a biomass dynamics model (BDM) and depletion-corrected average catch analysis (DCAC). The BDMs allowed me to use a range of life history parameter values in a Bayesian context to estimate current stock abundance and other important management parameters such as the maximum sustainable yield ( $MSY$ ), the fishing mortality rate that produces  $MSY$  ( $F_{msy}$ ), and the biomass that supports  $MSY$  ( $B_{msy}$ ). DCAC provides estimates of the potential yield ( $Y_{pot}$ ), a conservative estimate of  $MSY$ , and the sustainable yield ( $Y_{sust}$ ), or total removals that will maintain the stocks near or at their current level of abundance (MacCall, 2009). Until now, there has not been sufficient data to

assess stock status in either location. The ultimate goal of my research is to provide managers with assessment results that account for uncertainty in order to inform future big skate management.

## 2: METHODS

I used two methods to assess the big skate stocks in QCS and NHS: a Graham-Schaefer biomass dynamics model (BDM) and depletion-corrected average catch (DCAC) analysis. The Graham-Schaefer BDM provides estimates of current population abundance, the intrinsic growth rate of the population ( $r$ ), carrying capacity ( $K$ ), and management parameters. DCAC analysis outputs a potential yield based on unfished biomass and natural mortality, and an estimate of sustainable yield based on the current abundance. First, I will describe the Graham-Schaefer BDM followed by a description of the fishery-dependent and fishery-independent data used to fit the model. Second, I will describe Bayesian statistics, which I used to incorporate prior information. I took a Bayesian approach to fit a von Bertalanffy growth function (VBGF) to length-at-age data obtained from DFO research surveys. I used the VBGF parameters and probability distributions of natural mortality, age at maturity, and fecundity to estimate a measure of population productivity,  $r_{max}$ , through the Euler-Lotka model. I used the distribution of  $r_{max}$  to inform  $r$  of the Graham-Schaefer model for each stock. Third, I calculated posterior probability distributions for  $r$  and  $K$  of the Graham-Schaefer model in order to calculate management parameters: the maximum sustainable yield ( $MSY$ ), the biomass that supports  $MSY$  ( $B_{MSY}$ ), and the fishing mortality that results in  $MSY$  ( $F_{MSY}$ ). Fourth, I used DCAC to generate estimates of the potential and sustainable yields for each stock.

## 2.1 Biomass Dynamics Models

Biomass dynamic models (BDMs) allow users to estimate abundance and population growth rates from a time series of total catch and indices of abundance. I used the Graham-Schaefer BDM to calculate the abundance of the two big skate stocks,

$$B_{t+1} = B_t + rB_t \left(1 - \frac{B_t}{K}\right) - C_t \quad (1)$$

where  $B_t$  is the biomass of the stock at time  $t$ ,  $r$  ( $\text{year}^{-1}$ ) is the intrinsic growth rate of the population in the absence of density-dependence,  $K$  is the carrying capacity (tonnes), and  $C_t$  is catch in tonnes at time  $t$  (Schaefer, 1954; Hilborn and Walters, 1992). The Graham-Schaefer BDM allows for the direct estimation of management parameters such as maximum sustainable yield ( $MSY$ , equal to  $rK/4$ ), the biomass that sustains  $MSY$  ( $B_{MSY}$ , equal to  $K/2$ ), and the fishing mortality that results in  $MSY$  ( $F_{MSY}$ , equal to  $r/2$ ).

I parameterized the Graham-Schaefer BDM using commercial trawl and longline catch data, commercial trawl landings catch-per-unit-effort data, and fishery-independent indices of abundance from each stock location, all discussed in more detail below. I built all models in R 2.10.1 (R Development Core Team, 2009).

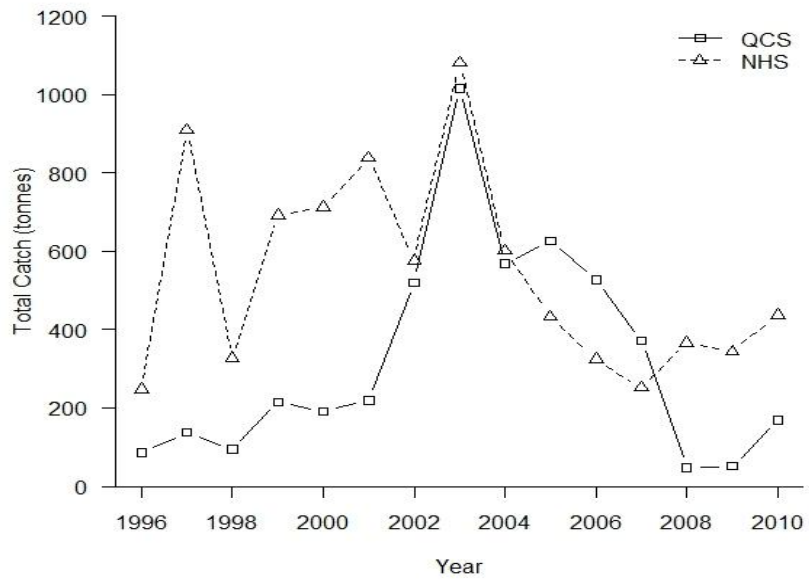
## 2.2 Fishery-Dependent Catch and Effort Data

Big skate catch data from QCS and NHS come from the trawl and longline sectors of the groundfish fishery (1996-2010). Trawl catch records prior to 1996 are not included in this assessment because the absence of onboard observers reduces the reliability of the data. Onboard observers recorded both landings and discards

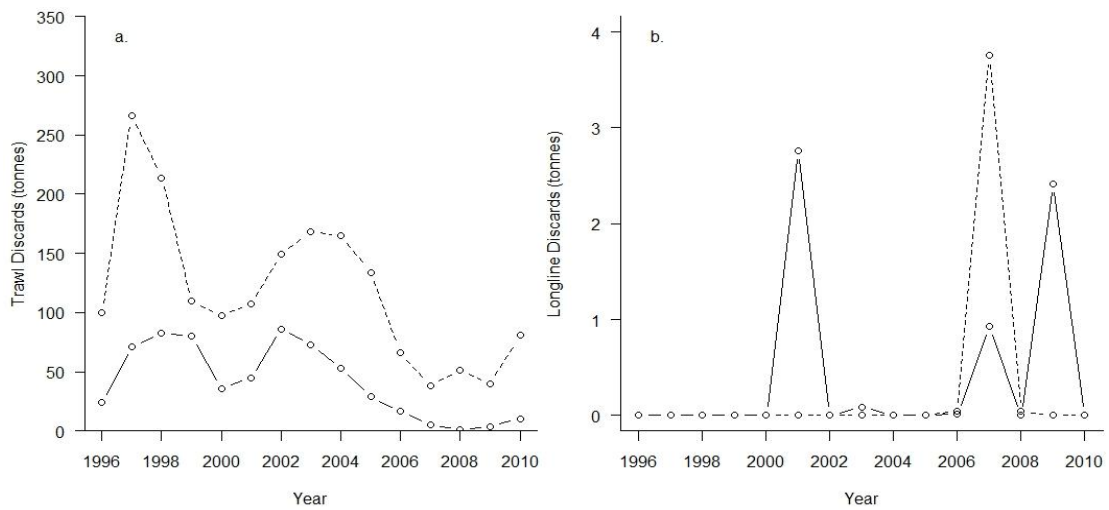
from 1996-2006. Observers classified discards further into four groups: marketable and dead, marketable and alive, unmarketable, or unknown. Onboard observers, logbooks, and dockside monitoring programs collected trawl landings and discards data from 2007-2010. Observers did not classify 2007-2010 discards into explicit categories as was done from 1996-2006. Longline catch data from 1996-2010 came from vessel logbooks and were classified as either landings or discards. Logbook data have been validated through an electronic monitoring system since 2006 (DFO, 2007).

In order to estimate the total catch-related mortality of big skate, I needed estimates of the biomass of skates that were caught, discarded at sea, and subsequently died. The data already contains the biomass caught and discarded at sea (discards), but the discard mortality, the percentage of catch thrown back that dies as a result of the capture and handling process (Alverson et al., 1994), is unknown. In order to estimate dead discards from the trawl and longline sectors in QCS and NHS, I assumed a 50% discard mortality rate based on reported discard mortality rates in the literature (50%, 45%, 40.9%, and 44% from Gertseva (2009), Enever et al. (2009), Laptikhovsky (2004) and Stobutzki (2002), respectively). I applied the 50% discard mortality rate to all discards from the longline sector, to all discards from the trawl sector from 2007-2010, and to trawl discards from 1996-2006 classified as “marketable and alive”, “unmarketable”, or “unknown”. I performed a sensitivity analysis using discard mortality rates of 0% and 100% to determine what effect, if any, my assumed discard mortality rate had on the model outcomes.

In order to fit the stock assessment model, I generated a time series of annual catch and fishery-dependent catch-per-unit-effort (CPUE) from 1996-2010. I calculated annual landings (tonnes) for each stock by summing the landings from each trawl tow and longline trip in a given year. Total catch is the sum of landings plus dead discards (Figure 5). I calculated dead discards in two ways depending on the data: (1) dead discards are the sum of total discards (e.g., trawl discards from 2007-2010) times the 50% discard mortality rate, or (2) dead discards are the discards recorded as dead upon release plus the 50% discard mortality rate applied to the sum of “marketable and alive”, “unmarketable”, and “unknown” discards. Figure 6 shows the total discards for each sector of the groundfish fishery in QCS and NHS. I assumed zero catch for NHS from 1984-1995 because the fishery-independent survey for NHS began in 1984. Therefore, model fitting begins in 1984 for NHS and 1996 for QCS. To calculate annual fishery CPUE (tonnes/hr), I summed the total landings for each trawl tow in a trip, divided by the hours spent trawling on that trip, and took the average across trips for each year (Figure 2). I technically calculated landings-per-unit-effort with the underlying assumption that big skate were a targeted, rather than a bycatch, species.



**Figure 5.** Total catch (landings plus dead discards) from the trawl and longline sectors of the groundfish fishery in QCS and NHS.



**Figure 6.** Total big skate discards (tonnes) in the trawl (a) and longline (b) sectors of the groundfish fishery for QCS (solid) and NHS (dashed). Note difference in axis scale for trawl and longline sector discards.

## **2.3 Survey Indices of Abundance**

I used three fishery-independent research trawl surveys as additional indices of abundance: QCS Shrimp Survey, QCS Synoptic Survey, and the Hecate Strait Multispecies Survey (Figures 3 and 4). The QCS Shrimp Survey occurred yearly from 1998-2009, the QCS Synoptic Survey occurred yearly from 2003-2005 and then every two years until 2009, and the Hecate Strait Multispecies survey ran from 1984-2003 although not every year (DFO, 1999; Chromanski et al., 2004). All three surveys recorded tow duration (minutes), trawl door spread (meters), vessel speed (meters per minute), big skate weight (kg), and big skate density ( $\text{kg}/\text{m}^2$ ). I only used positive tows (those that encountered big skate) to calculate CPUE (tonnes/hr) because all three surveys were heavily zero-inflated. I summed the total landings for each trawl tow in a trip, divided by the hours spent trawling on that trip, and took the average across trips for each year to calculate survey CPUE.

## **2.4 Bayesian Approach to Parameter Estimation**

I took a Bayesian approach in order to include information from previous research and expert opinion. Bayes theorem, the basis for Bayesian statistics, describes the relationship between two conditional probabilities and calculates the probability of one event occurring given that another event has already occurred (Bayes, 1763). In Bayesian statistics, where Bayes' theorem is used for statistical inference, a range of possible parameter values are treated as one event and the observed data are treated as the other (Cooper and Miller, 2007). Bayesian statistics consists of three components: the prior probability distribution of the parameter values in question before the data are observed, the likelihood of the observed data,



and the posterior probability distribution of the parameter values given the observed data (McAllister et al., 1994). Bayes theorem for use in statistical inference is written as,

$$P(\theta_i|Data) = \frac{L(\theta_i|Data)p(\theta_i)}{\int L(\theta_i|Data)p(\theta)d\theta} \quad (2)$$

where the posterior probability distribution ( $P$ ) of the parameters ( $\theta_i$ ) given the observed data ( $Data$ ) is equal to the likelihood ( $L$ ) of the parameters given the observed data ( $L(\theta_i|Data)$ ) multiplied by the prior probability distribution of the parameters ( $p(\theta_i)$ ) divided by the marginal probability distribution ( $\int L(\theta_i|Data)p(\theta)d\theta$ ) (McCallister et al., 1994; Cooper and Miller, 2007). Since the denominator in Equation 2 is generally used as a scaling constant, the posterior probability distribution of the parameter(s) is proportional to the likelihood of the parameters given the observed data multiplied by the prior probability of the parameters (Ellison, 1996). Bayesian methods combine knowledge known prior to data collection with observed data to calculate posterior probabilities associated with alternate hypotheses (McAllister and Kirkwood, 1998).

The prior probability distribution of a parameter is the degree of belief associated with a range of possible parameter values estimated from previous research or determined using expert opinion (Punt and Hilborn, 1997). Priors may be non-informative, containing little to no information about the parameter(s) in question, or they may be informative, and reflect established information about the species in question, a similar species, or a similar environment. Parameter uncertainty can be expressed by a probability distribution where the shape of the distribution reflects the degree of belief on a range of parameter values (Walters and Ludwig, 1994). A

uniform distribution is flat and assumes all parameter values within a range are equally probable. Some distributions, such as normal or certain beta distributions, are shaped such that some parameter values are more probable than others. The likelihood of the parameters given the observed data is the probability of obtaining the data given a set of parameter values assumed to be true (McAllister and Kirkwood, 1998). Equation 2 combines the information contained in the prior distribution with the information contained in the observed data to estimate a posterior probability distribution of the parameter in question. Informative priors can strongly influence the shape of the posterior distribution, especially when the observed data contains little information. However, if the information contained in the data dominates the prior, then the posterior distribution will reflect the shape of the likelihood (Ellison, 1996).

## 2.5 Bayesian Approach to Estimate $r_{max}$ from a Growth Curve

I used length-at-age data gathered from 125 female big skate caught on DFO research surveys to fit a von Bertalanffy growth function (VBGF)(McFarlane and King, 2006; King and McFarlane, 2010) . The three parameter VBGF is,

$$L_a = L_\infty * \left( 1 - e^{-k(a-t_0)} \right) \quad (3)$$

where  $L_\infty$  (mm) is the maximum asymptotic length ,  $L_a$ (mm) is length at age  $a$ ,  $k$  ( $\text{year}^{-1}$ ) is the Brody growth coefficient which measures how quickly an organism reaches the asymptotic length, and  $t_0$ (years) is the theoretical negative age when length equals zero(von Bertalanffy, 1938; Beverton and Holt, 1959). I fit the VBGF using Bayesian methods to include prior information from previous biological studies on big skate. I rescaled a beta ( $\alpha=1$ ,  $\beta=1$ ) distribution for the priors on  $k$  and  $t_0$  which

approximates a uniform distribution within a specified range. I based the range of the priors for  $k$  (0.01-0.30 year<sup>-1</sup>, Eq. 4) and  $t_0$  (-0.01 – -3 years, Eq. 5) on values published in the literature for big skate (Zeiner and Wolf, 1993; Benson et al., 2001; Gburski et al., 2007). I rescaled a beta ( $\alpha=1.1, \beta=1.1$ ) distribution for the  $L_\infty$  prior which gave slightly lower likelihood to the lower and upper bounds of the distribution to assist the model in fitting to the data (Figure 7). The prior for  $L_\infty$  ranged between 2000 and 3500 mm based on maximum lengths reached by skates with similar biology to the big skate (Eq. 6). Although the largest skate in the world, the common skate (*Dipturus batis*), reaches a total length of 2850 mm (Froese and Pauly, 2011), I extended the prior distribution past this length to allow the data to shape the posterior.

$$p\left(\frac{L_\infty - 2000}{3500 - 2000}\right) \sim \text{beta}(\alpha=1.1, \beta=1.1) \quad (4)$$

$$p\left(\frac{k-0.01}{0.30-0.01}\right) \sim \text{beta}(\alpha=1, \beta=1) \quad (5)$$

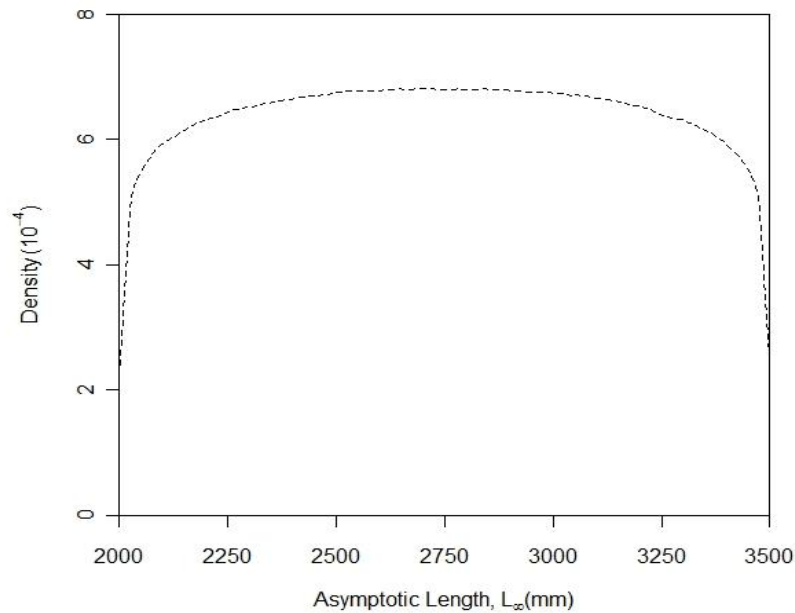
$$p\left(\frac{t_0 + 3}{-0.01 + 3}\right) \sim \text{beta}(\alpha=1, \beta=1) \quad (6)$$

I assumed lognormally distributed error for the VBGF (Siegfried and Sanso, 2006). Therefore, the likelihood component of the Bayesian model, written in terms of the negative log-likelihood is,

$$-\log L(L_\infty, k, t_0, \sigma^2 | y) = -\log\left(\frac{1}{y\sqrt{2\pi\sigma^2}}\right) + \frac{1}{2\sigma^2} (\log(y) - \log(\hat{y}))^2 \quad (7)$$

where  $L$  is the likelihood of the parameters  $L_\infty$ ,  $k$ ,  $t_0$ , and  $\sigma^2$  given the observed length-at-age data,  $y$ , and  $\hat{y}$  is the predicted length-at-age calculated using the VBGF

(Eq.3). The total negative log-likelihood is the sum of the negative log-likelihood (Eq. 7) times the prior probability distributions of the three VBGF parameters (Eqs. 4-6).



**Figure 7.** Prior probability distribution for the maximum asymptotic length,  $L_{\infty}$ , bounded between 2000-3500 mm.

I generated a posterior probability distribution for each parameter by combining the prior probability distributions of VBGF parameters and the likelihood of the parameters given the observed length-at-age data via Markov Chain Monte Carlo (MCMC) using the MCMCmetrop1R function in R (Martin and Quinn, 2005). MCMC uses a random walk algorithm, in this case the Metropolis-Hastings, to sample from the posterior probability distribution (McAllister and Kirkwood, 1998; Gelman et al., 2004). I initialized the MCMC chain for each of the three VBGF parameters at the best-fit parameter values, those which maximize the likelihood, determined by `optim()` in R. I drew 20 million iterations from each parameter's MCMC chain with a burn-in period of 2,000 iterations and thinning by 500 to produce 40,000 samples. I

tested each parameter's MCMC chain for convergence using the Geweke diagnostic and verified that within chain autocorrelation was below 0.20 using the CODA package in R (Plummer et al., 2006).

I used the  $L_{\infty}$  and  $k$  posterior distributions to calculate a posterior distribution for natural mortality ( $M$ ) using Pauly's (1980) equation,

$$\log M = \alpha - \beta * \log(L_{\infty}) + \gamma * \log(k) + \delta * \log(T) \quad (8)$$

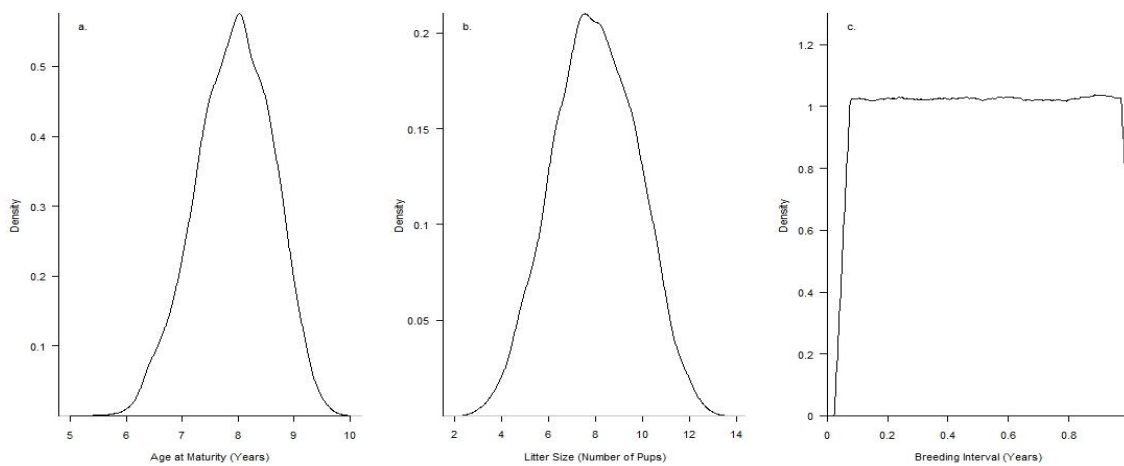
where  $L_{\infty}$  and  $k$  are parameters of the VBGF,  $T$  is the mean environmental temperature in the location of the stock and  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$  are model coefficients with values of -0.0066, 0.279, 0.6543, and 0.4634, respectively. I used Pauly's (1980) equation for natural mortality because the inclusion of temperature may provide more reliable estimates of  $M$  as temperature is the most important abiotic factor affecting an organism's biological rates (Charnov and Gillooly, 2004; Quiroz et al., 2010). For my model, I drew temperature values from a uniform distribution between 9 and 11°C based on sea surface temperatures at McInnes Island, British Columbia (McQueen and Ware, 2006). In order to account for correlation between the model coefficients ( $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$ ) of Pauly's (1980) equation, a linear model was fit to the original data from Pauly (1980) using Eq. 8. The model coefficients,  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$ , were then drawn from a multivariate normal distribution using the re-fit model's covariance matrix (Pardo et. al., 2010). I applied the 40,000 posterior distribution estimates of  $L_{\infty}$  and  $k$  available from each parameter's MCMC chain, 40,000 random draws from the uniform temperature distribution, and 40,000 draws of re-fit model coefficients to Eq. 8 to produce a probability distribution of  $M$ .

I calculated a distribution for  $r_{max}$  using probability distributions of natural mortality, age at maturity, and fecundity. I rescaled a beta ( $\alpha=7$ ,  $\beta=5$ ) distribution for the age at maturity such that it was bounded between 5 and 9 years with a peak of 8 years (Figure 8a). The distribution for age at maturity captures the current knowledge that big skate females in BC mature at age 8 but mature individuals as young as 5 and immature females as old as 9 are known to occur (McFarlane and King, 2006). Female fecundity is half the litter size ( $l$ , number of pups) divided by breeding interval ( $i$ , years), assuming a 1:1 sex ratio. Due to the uncertainty surrounding the true values of  $l$  and  $i$ , I used a rescaled beta probability distribution for litter size (Figure 8b) and a uniform distribution for breeding interval (Figure 8c) in lieu of point estimates. The distribution of  $l$  is bounded between 2 and 14 but peaks at 8 because big skate simultaneously release two eggs cases with 1-7 embryos per case, but more commonly with 3-4 (Ebert, 2003). The distribution of  $i$  assumes that big skate can deposit eggs as often as every 2 weeks or as infrequently as once a year (Ebert, 2003). The range of  $i$  used here is plausible as skates and rays are known to produce eggs throughout most of the year (Hoenig and Gruber, 1990).  $r_{max}$  is calculated using the Euler-Lotka equation (Myers and Mertz, 1998),

$$b = e^{F_{extinct}(\alpha - \alpha_{sel} + 1)} (1 - e^{-(M + F_{extinct})}) \quad (9)$$

where  $b$  is fecundity,  $F_{extinct}$  ( $\text{year}^{-1}$ ) is the fishing mortality required to drive a population to extinction,  $\alpha$  is the age at maturity,  $\alpha_{sel}$  is the age at selectivity to the fishery, and  $M$  is natural mortality ( $\text{year}^{-1}$ ).  $F_{extinct}$  equals  $r_{max}$  when the age of selectivity equals 1 (Myers and Mertz, 1998; Dulvy et al., 2004; Garcia et al., 2008). An age of selectivity of 1 is realistic for big skate since they are born large enough to

be caught through trawl fisheries. I generated a distribution of  $r_{max}$ , by iteratively solving Eq. 9 for  $F_{extinct}$  using unique combinations of  $\alpha$ ,  $b$ , and  $M$  in order to create a prior probability distribution for the intrinsic growth rate,  $r$ , of the Graham-Schaefer model. I tested the sensitivity of  $r_{max}$  to varying ages of selectivity to determine how  $r_{max}$  would change if my assumption regarding age of selectivity was underestimated.



**Figure 8.** Density distributions for age at maturity (years, a), litter size (number of pups, b), and breeding interval (years, c) used in the calculation of  $r_{max}$ .

## 2.6 Abundance and Management Parameter Estimation using BDMs

I developed prior probability distributions for the three Graham-Schaefer BDM parameters: intrinsic growth rate ( $r$ ), carrying capacity ( $K$ ), and *depletion* which estimates biomass at the start of the fishery as a proportion of  $K$  (Punt, 1990). Both big skate stocks may have been at some fraction of  $K$  in 1996 because the groundfish fishery began around 1954, and although not targeted, big skate landings and discards may have occurred. The prior for  $r$ , aimed to match the distribution of

$r_{max}$ , was best represented by a rescaled beta ( $\alpha=3$ ,  $\beta=15$ ) distribution bounded between 0.25-0.90 year<sup>-1</sup>(Eq. 10). The prior for  $K$  was a rescaled beta ( $\alpha=1.15$ ,  $\beta=1.15$ ) distributed between 1,000 and 10 million tonnes (Eq. 11). The wide, slightly informative distribution for  $K$  attempted to give the model flexibility to find the most probable value given the data. *Depletion* was uniformly distributed between 0 and 1 (Eq. 12).

$$p\left(\frac{r-0.25}{0.90-0.25}\right) \sim \text{beta}(\alpha =3, \beta=15) \quad (10)$$

$$p\left(\frac{K-1000}{1e7-1000}\right) \sim \text{beta}(\alpha =1.15, \beta=1.15) \quad (11)$$

$$p(\text{depletion}) \sim \text{beta}(\alpha = 1, \beta=1) \quad (12)$$

Each stock's BDM fit the indices of population abundance by applying an observation error estimator that assumed all error was present in the relationship between stock abundance and the index of abundance (Polachek et al., 1993; Hayes et al., 2009). The equation used to calculate the predicted index of abundance is,

$$I_{j,t} = q_j B_t \quad (13)$$

where  $I_{j,t}$  is the value of the abundance for index  $j$  at time  $t$ , and  $q$  is the catchability coefficient which scales the population size to the index  $j$ . The observation error likelihood estimates the difference between the observed index of abundance and the predicted index calculated through the model (Brodziak and Ishimura, 2011). A value for  $\sigma$  was calculated for each index of abundance,  $j$ , using the equation,

$$\sigma_j = \sqrt{\frac{\sum_1^t (\log(I_{j,t}) - \log(\hat{I}_{j,t}))^2}{n}} \quad (14)$$



where  $\widehat{l}_{j,t}$  is the predicted index, calculated from the predicted  $q$  and predicted biomass using Eq. 13, and  $n$  is the number of data points in the index time series. I used the negative log-likelihood to determine the relative fit of the BDMs to the catch, CPUE, and survey data. I calculated the negative log-likelihood for each index of abundance assuming log-normal error.

$$-\log L(q_j, r, K, \text{depl}, \sigma_j / l_{j,t}) = -\log \left( \frac{1}{l_{j,t} \sqrt{2\pi\sigma_j^2}} \right) + \frac{1}{2\sigma_j^2} (\log(l_{j,t}) - \log(\widehat{l}_{j,t}))^2 \quad (15)$$

The total negative log-likelihood was the sum of the negative log-likelihood of each available index (Eq. 15) multiplied by the prior probability distributions of the three Graham-Schaefer BDM parameters (Eqs. 10-12).

I used MCMC to sample from the posterior probability distributions of the three BDM parameters. I drew 20 million iterations from each parameter's MCMC chain, with a burn-in of 2,000 and thinning by 1,000 for a total chain length of 19,998. I checked MCMC diagnostics to verify chain convergence on the posterior distribution of the parameters. I calculated probability distributions of management parameters of interest ( $MSY$ ,  $B_{MSY}$ , and  $F_{MSY}$ ) using the posterior probability distributions of  $r$  and  $K$ . I used each iteration of the MCMC chain to calculate the predicted big skate population in each stock for the length of the time series along with 50, 80 and 90% quantiles. Additionally, I used the median of the posterior distribution for the three parameters to calculate predicted indices of abundance for each stock.

## 2.7 Depletion-Corrected Average Catch (DCAC)

The final component of the stock assessment was the use of depletion corrected average catch analysis (DCAC) to calculate the potential yield ( $Y_{pot}$ ) and sustainable

yield ( $Y_{sust}$ ) of big skate in QCS and NHS (MacCall, 2009).  $Y_{pot}$  is a conservative estimate of  $MSY$  based on unfished biomass and natural mortality, and the  $Y_{sust}$  is the total removals that will maintain a stock at its current abundance given its depletion over the catch time series. The calculations of  $Y_{pot}$  and  $Y_{sust}$  require a time series of catch, an estimate of natural mortality ( $M$ ), the ratio of  $F_{MSY}$  to  $M$  ( $c$ ), and delta ( $\Delta$ ), the reduction in vulnerable biomass over the catch time series as a fraction of the unfished biomass,  $B_0$ . Larger positive values of  $\Delta$  signify greater reductions to stock size; negative values indicate a population that has increased over time (Berkson et al., 2011). The first step to calculating  $Y_{sust}$  requires the calculation of  $Y_{pot}$ . The equation used to calculate potential yield is,

$$Y_{pot} = 0.4 * c * M * B_0 \quad (16)$$

The term,  $c * M$  replaces the assumption that  $F_{MSY} = M$  since studies have found that this assumption may actually overestimate the fishing mortality a stock can withstand (MacCall, 2009). I used the posterior distribution of  $F_{MSY}$  calculated from the BDM in lieu of  $c * M$ . Additionally, I used the posterior probability distribution of  $K$  from the BDM component as  $B_0$ . Therefore, the equation I used to calculate  $Y_{pot}$  is,

$$Y_{pot} = 0.4 * F_{MSY} * K \quad (17)$$

I used the posterior probability distributions of  $F_{MSY}$  and  $K$  to calculate  $Y_{pot}$  in order to capture the uncertainty surrounding the true values of  $K$  and  $F_{MSY}$ .  $Y_{pot}$  is a conservative estimate of  $MSY$  because according to Equation 17,  $B_{MSY}$  is equal to 40% of  $K$  as opposed to 50% of  $K$  assumed in the logistic Graham-Schaefer model.

Ultimately, I used DCAC to determine the sustainable yield ( $Y_{sust}$ ) that can be removed from the stock while maintaining its current abundance. The sustainable

yield takes into account a “windfall” ratio which represents the reduction of biomass from  $B_0$  to  $B_{MSY}$ . The equation for the sustainable yield is,

$$Y_{sust} = \frac{\sum C}{n + \frac{W}{Y_{pot}}} \quad (18)$$

where  $C$  are the catches in the time series,  $n$  is the number of years in the catch time series, and the ratio of  $W/Y_{pot}$  ( $= \Delta/0.4 * F_{MSY}$ ) expresses the windfall relative to a single year of potential yield. If no change in abundance occurred (i.e.,  $\Delta=0$ ), the equation for  $Y_{sust}$  equals the average catch. If stock abundance increased,  $\Delta$  and the ratio  $W/Y_{pot}$  are negative and  $Y_{sust}$  is larger than average historical catches (McCall, 2009).  $\Delta$  is calculated using the equation,

$$\Delta = B_{FYR} - B_{LYR} / B_0 \quad (19)$$

where  $B_{FYR}$  is the biomass in the first year of the time series,  $B_{LYR}$  is the biomass in the last year of the time series, and  $B_0$  is the unfished biomass (MacCall, 2009). I used the predicted first and last year biomass from each stock’s BDM to calculate the difference in biomass for each stock over the time series. I also used the posterior probability distribution of  $K$  from the BDMs as the unfished biomass to calculate a posterior distribution of  $\Delta$ . According to the BDM predictions of first and last year biomass and  $K$ , the 95% quantile of  $\Delta$  for QCS was -0.65 - -0.01 from 1996-2010 and -0.89-0.0003 for NHS from 1984-2010. I drew random values of  $\Delta$  directly from the posterior estimates for each stock. The 95% quantiles of  $\Delta$  for both stocks are negative values thereby predicting that both stocks have increased over their respective catch time series. However, the full ranges of  $\Delta$  for both stocks include zero (i.e., same biomass at first and last year) and positive estimates (i.e., decreasing biomass over the time series). The estimates of  $Y_{sust}$  predicted by my

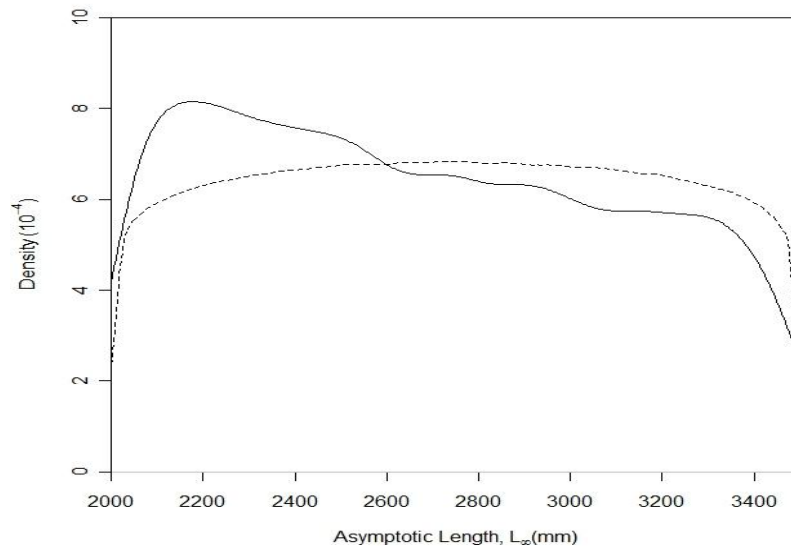
assumed range of  $\Delta$ s consider the uncertainty contained in BDM outputs. I interpreted the estimated  $Y_{sust}$  values given the stock abundance estimated by each stock's BDM.

## 3: RESULTS

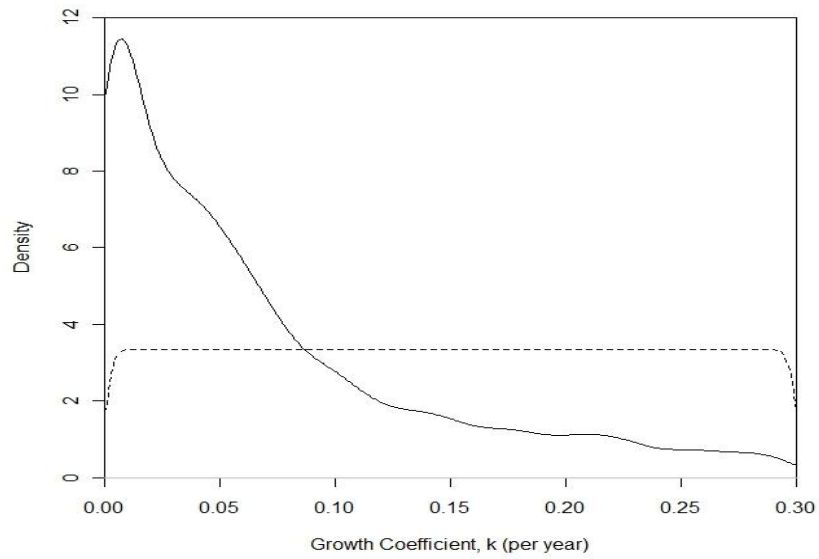
### 3.1 Bayesian Approach to Estimate $r_{max}$ from a Growth Curve

The posterior probability distributions of the von Bertalanffy growth function (VBGF) parameters suggest that the data contained little information to improve estimates of the asymptotic length,  $L_{\infty}$ , but greatly improved estimates of the growth rate,  $k$ , and age when length equals zero,  $t_0$ . The observed female length-at-age data contained some information regarding the most likely value of  $L_{\infty}$  as shown by the slight difference between the shape of the prior and posterior probability distributions (Figure 9). A complete overlap between the prior and posterior probability distributions would indicate that the data did not provide any additional information to shape the posterior distribution. The skewed posterior distributions of  $k$  and  $t_0$  are evidence that the data informed the shape of those posterior distributions since the prior distributions used for both parameters were flat (Figures 10 and 11). However, the inverse correlation that exists between  $L_{\infty}$  and  $k$  may be a factor in the highly skewed shape of the  $k$  posterior. The estimates of the mode of the  $L_{\infty}$ ,  $k$ , and  $t_0$  posterior distributions equalled 2177 mm, 0.007 year<sup>-1</sup>, and -0.021 years, respectively. The median estimates of the posterior distributions ( $L_{\infty}$  = 2647 mm,  $k$  = 0.044 year<sup>-1</sup> and  $t_0$  = -0.094 years) consistently underestimate predicted lengths-at-age (Figure 12). Percentiles, means, and standard deviations of the three VBGF parameter posterior values are shown in Table 1.

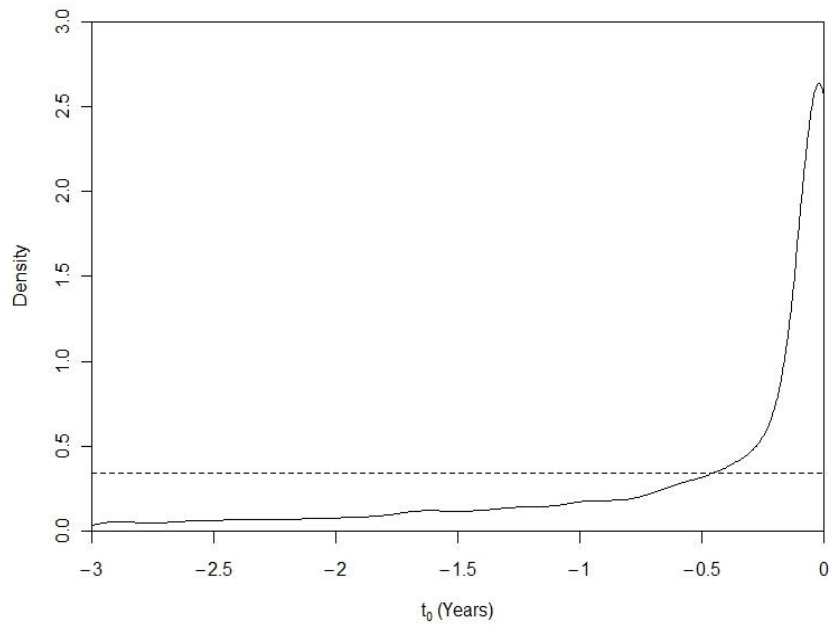
The posterior distributions of  $L_\infty$  and  $k$  produced a wide distribution of natural mortality,  $M$ , whereas the distribution of population productivity,  $r_{max}$ , based on life history parameters was highly informative.  $M$  ranged from 0.00035-0.347 year<sup>-1</sup> with a mode equal to 0.007 year<sup>-1</sup>(Figure 13). The skewed shape of the  $M$  distribution may be due to the skewed shape of the  $k$  posterior used in its calculation.  $r_{max}$  exhibited a tight distribution around the mode of 0.356 year<sup>-1</sup> and ranged from 0.223-0.772 year<sup>-1</sup> (Figure 14).The shape of the distribution for  $r_{max}$  closely matches the distributions of age at maturity and litter size used in its calculation. Table 2 shows the 2.5, 25, 50, 75 and 97.5% quantiles, mean, and standard deviation of  $M$  and  $r_{max}$ . The sensitivity analysis on the age of selectivity assumption shows that increasing the age of selectivity while holding all other parameters constant increases the mean and standard deviation of  $r_{max}$ (Figure 15).



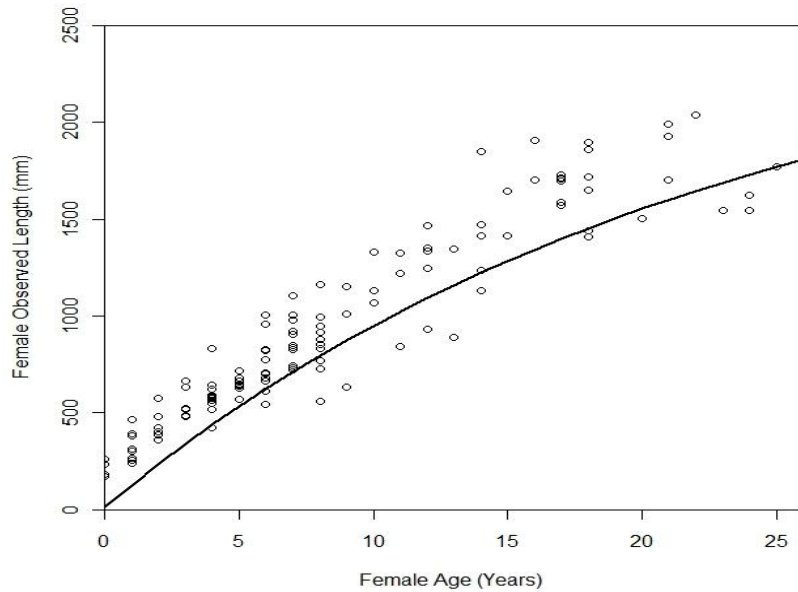
**Figure 9.** Prior (dashed line) and posterior (solid line) probability distributions for  $L_\infty$  of the VBGF.



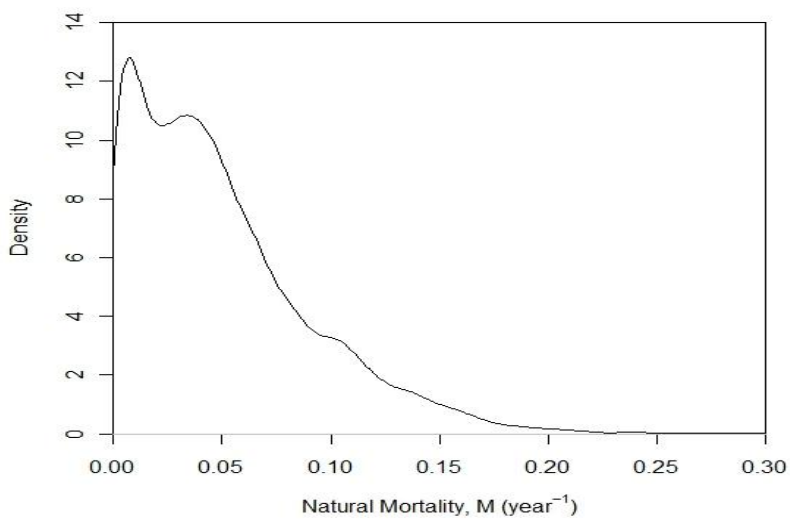
**Figure 10.** Prior (dashed line) and posterior (solid line) probability distributions of  $k$ , the growth rate of the VBGF.



**Figure 11.** Prior (dashed line) and posterior (solid line) probability distributions for  $t_0$  of the VBGF.

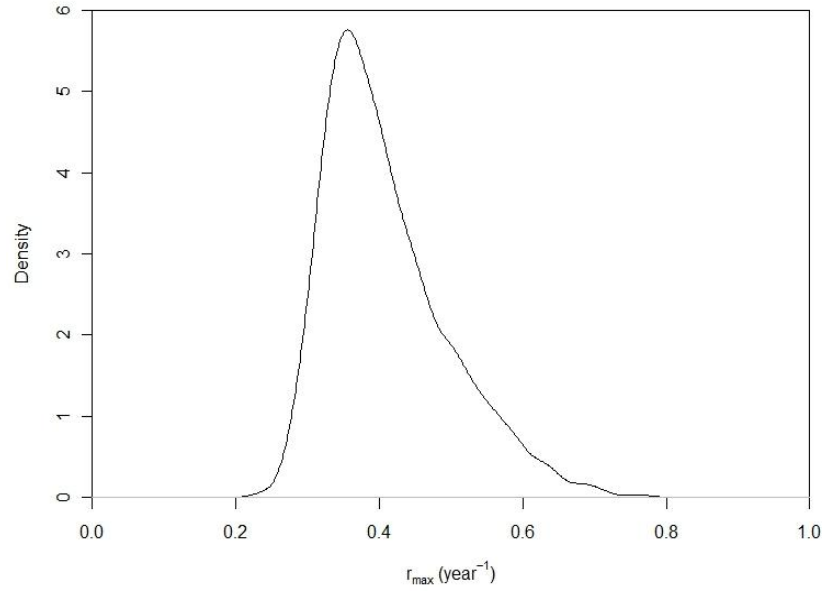


**Figure 12.** Observed (empty circles) versus predicted (solid line) length-at-age data for female big skate calculated using the median estimates from  $L_{\infty}$ ,  $k$ , and  $t_0$  posterior distributions.

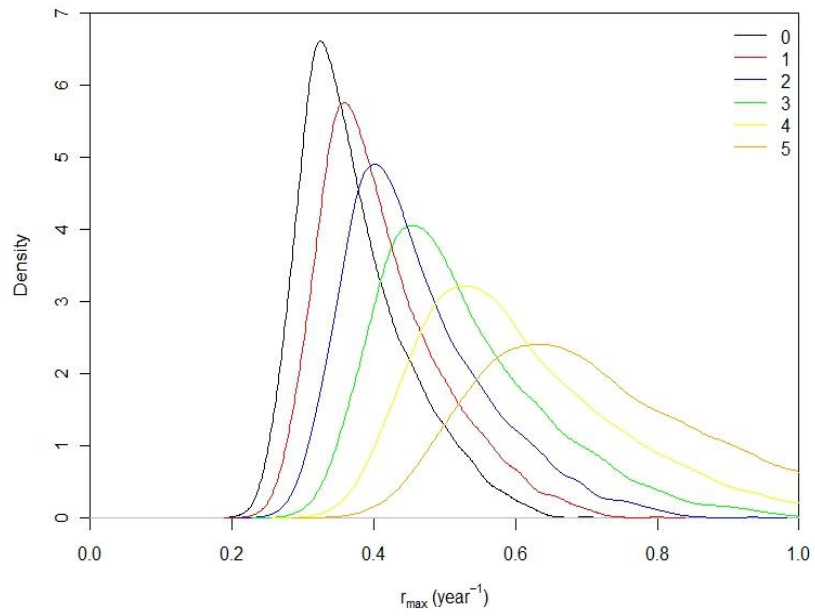


**Figure 13.** Density plot of annual natural mortality,  $M$ , calculated using Pauly's (1980) equation (Eq. 8).





**Figure 14.** Density plot of  $r_{max}$  calculated by iteratively solving Eq. 11 using natural mortality, age at maturity, fecundity, and age of selectivity.



**Figure 15.** Probability distribution of  $r_{max}$  under different ages of selectivity (years) to the fishery.

**Table 1.** Statistics from the posterior distributions of the three VBGF parameters sampled through MCMC .

Parameter	2.50%	25%	Median	75%	97.50%	Mean	SD
$L_{\infty}$ (mm)	2041	2331	2660	3023	3433	2687	413
k	0.00	0.01	0.04	0.09	0.26	0.06	0.07
$t_0$ (years)	-2.48	-0.49	-0.04	0.00	0.00	-0.40	0.68

**Table 2.** Statistics from the probability distributions of natural mortality,  $M$ , and

Parameter	2.50%	25%	Median	75%	97.50%	Mean	SD
$M$ (year <sup>-1</sup> )	0.001	0.016	0.038	0.068	0.149	0.047	0.040
$r_{max}$ (year <sup>-1</sup> )	0.288	0.347	0.391	0.457	0.618	0.409	0.085

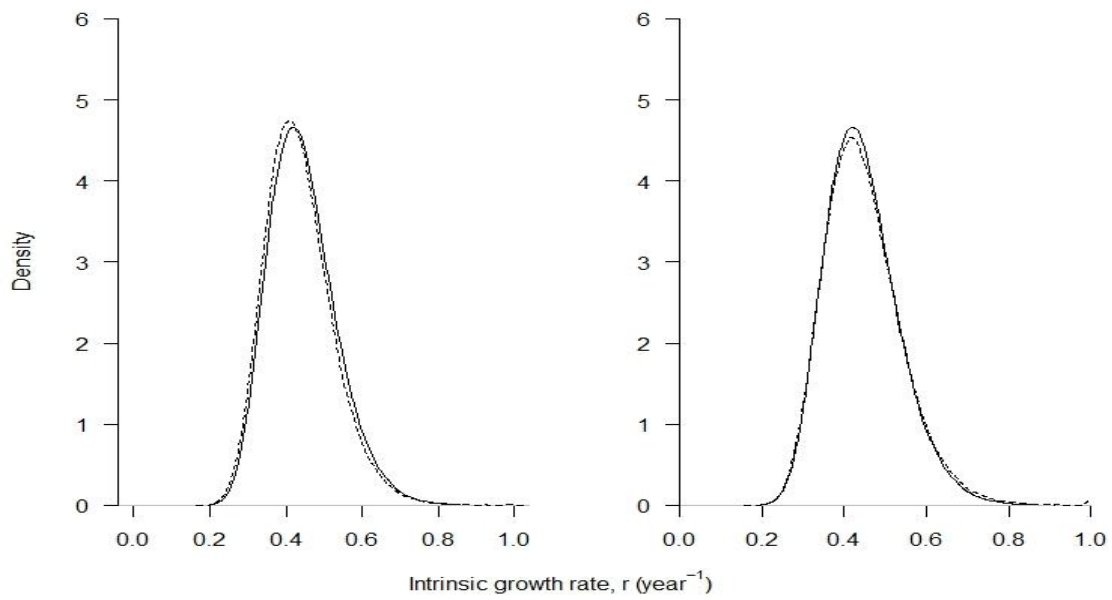
### 3.2 Management Parameter and Abundance Estimation Using BDMs

The highly informative prior probability distribution for the intrinsic growth rate,  $r$ , influenced the posterior probability distributions for all three parameters of the Graham-Schaefer biomass dynamics model. For both stocks, the prior and posterior probability distributions completely overlapped signifying a lack of information in the observed data (i.e., total catch, trawl landings CPUE, and research survey data) regarding the true value of  $r$  (Figure 16). The lack of contrast in the data set for each stock produced similar modes for the posterior probability values of  $r$  equal to 0.366 year<sup>-1</sup> and at 0.359 year<sup>-1</sup> for QCS and NHS, respectively. The modes of the posterior of  $r$  from each stock are almost equal to the peak  $r_{max}$  (0.356 year<sup>-1</sup>) used to define the prior probability distribution of  $r$ , further evidence that the observed data did not update the posterior distribution. The posterior distributions of the carrying capacity,  $K$ , for both stocks were highly skewed towards higher abundances, likely a result of the inverse relationship

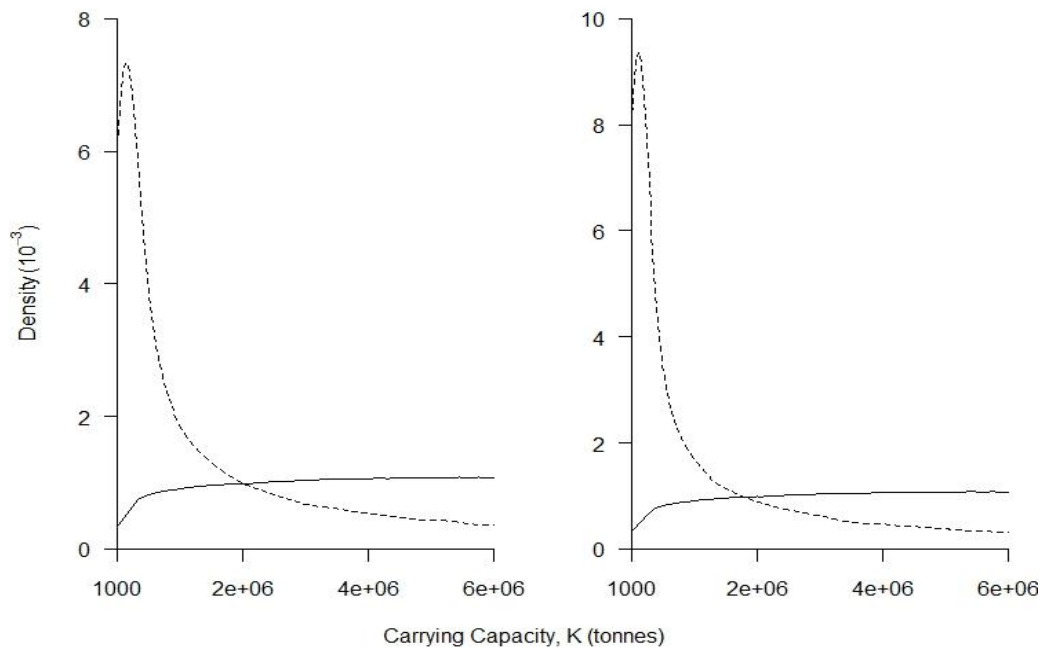
between  $r$  and  $K$  (Figure 17). The modes of the posterior probability estimates of  $K$  occurred at approximately 202,000 tonnes for QCS and 159,000 tonnes for NHS. The mode of the *depletion* posterior distribution for QCS and NHS signified that at the start of the targeted fishery in 1996 the stocks were at 72% and 78% of  $K$ , respectively (Figure 18). The depletion results suggest that non-targeted big skate mortality induced through other fisheries prior to 1996 is a possibility. The median estimates of  $r$ ,  $K$ , and *depletion* occurred at 0.385 year<sup>-1</sup>, 698,000 tonnes, and 68% for QCS and 0.391 year<sup>-1</sup>, 501,000 tonnes, and 62% for NHS. Quantiles, means, and standard deviations for the three BDM parameters for each stock are shown in Table 3 and 4 for QCS and NHS, respectively.

Posterior distributions of  $MSY$  and  $B_{MSY}$  exhibited high uncertainty whereas  $F_{MSY}$  was highly informative. The mode of the posterior for  $MSY$  for QCS was higher than that for NHS, 21,800 tonnes versus 16,200 tonnes, respectively (Figure 19).  $B_{MSY}$  is directly related to  $K$ ; therefore, the posterior distributions and modes of  $B_{MSY}$  in each stock exactly match that of  $K$ , except the values are halved (Figure 20). The long tails present in the  $MSY$  and  $B_{MSY}$  posterior distributions are due to the highly skewed posterior for  $K$  because it factors into both management parameter calculations ( $MSY=r*k/4$  and  $B_{MSY}=K/2$ ). Posterior distributions for  $F_{MSY}$  in each stock are directly related to the posterior distributions for  $r$  and as a result also exhibit tight distributions about their modes (Figure 21). Quantiles, means, and standard deviations for the three management parameters are shown in Table 5 and 6 for QCS and NHS, respectively.

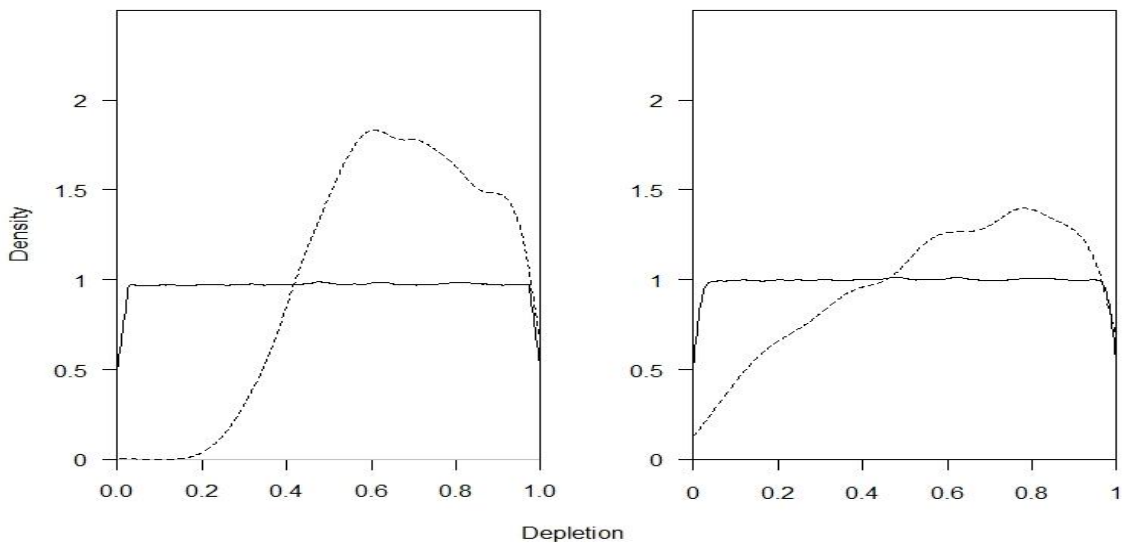
Both QCS and NHS stocks had median predicted population abundances at their carrying capacities. It is unlikely that the stocks are currently overfished (as of 2010) as the median estimated population size is well above the estimated  $B_{MSY}$ . The median predicted population biomass for QCS started at 474,000 tonnes in 1996 and slowly increased to its final predicted biomass of 698,000 tonnes. For NHS the predicted population biomass was 313,000 tonnes in 1984 and stabilized at its final predicted biomass of 501,000 tonnes (Figure 22). The predicted indices for QCS increased and then levelled off through the available data points. The fit predicted by the BDM concerning the QCS stock results from the lack of a trend in the later part of the CPUE time series and the contrasting trends seen in the two fishery-independent indices of abundance (Figure 23). Similarly, the CPUE time series and the Hecate Strait Multispecies survey for the NHS stock was highly variable and showed little trend; hence, the model fit a horizontal line through the later part of the time series (Figure 24).



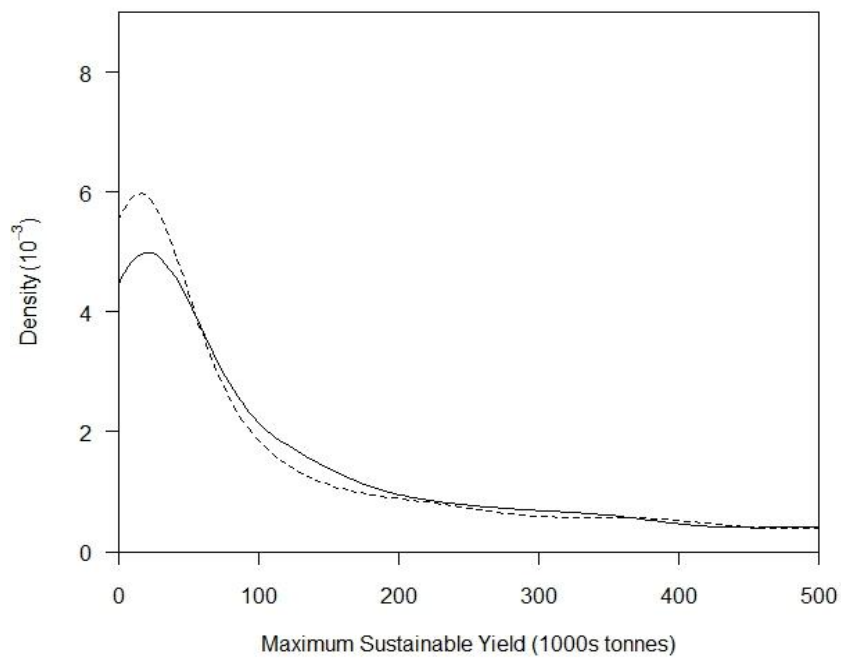
**Figure 16.** Prior (solid line) and posterior (dashed line) probability distributions for the intrinsic growth rate for QCS (left) and NHS (right).



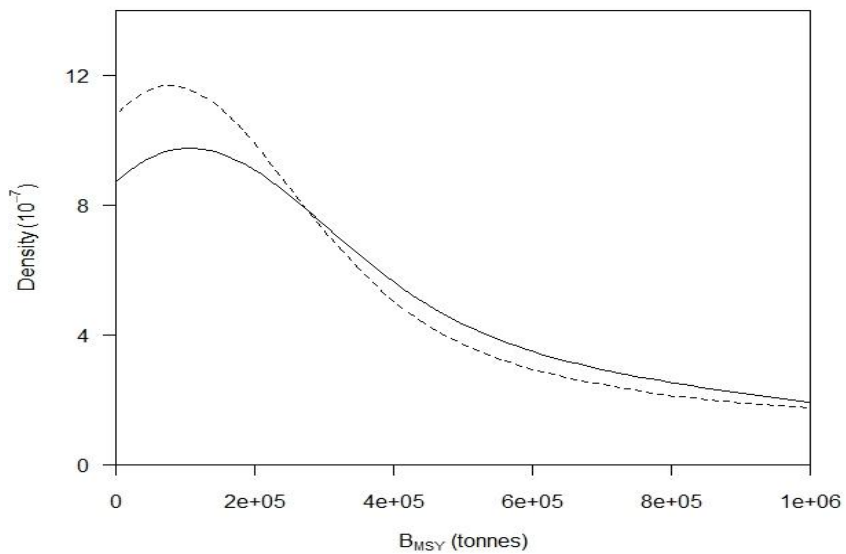
**Figure 17.** Prior (solid line) and posterior (dashed line) probability distributions of the carrying capacity,  $K$ , for QCS (left) and NHS (right). X-axes were truncated to show shape of posterior at lower abundances as the posterior distribution did not change at abundances larger than 6,000,000 tonnes.



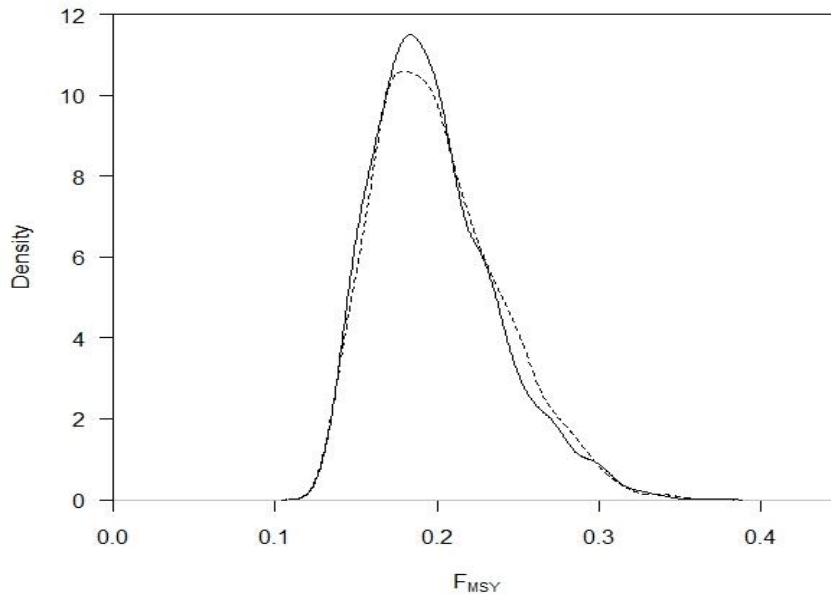
**Figure 18.** Prior (solid line) and posterior (dashed line) probability distributions for the depletion parameter of the Graham-Schaefer biomass dynamics model for QCS (left) and NHS (right).



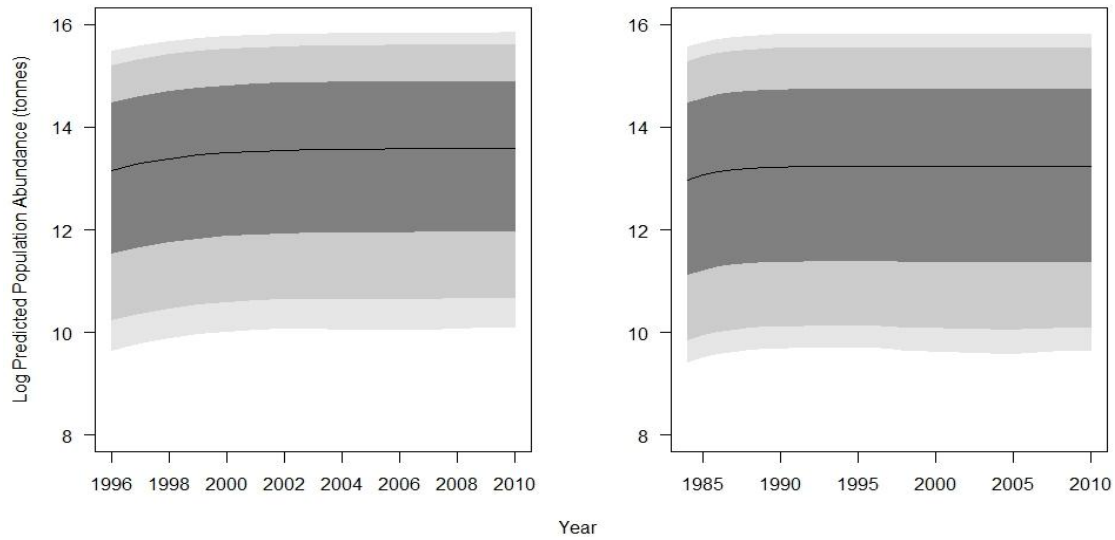
**Figure 19.** *MSY* posterior probability distribution for QCS (solid line) and NHS (dashed line) stocks measured in 1,000s of tonnes.



**Figure 20.** Posterior distribution of the biomass that sustains *MSY*,  $B_{MSY}$  (tonnes), for QCS (solid line) and NHS (dashed line).

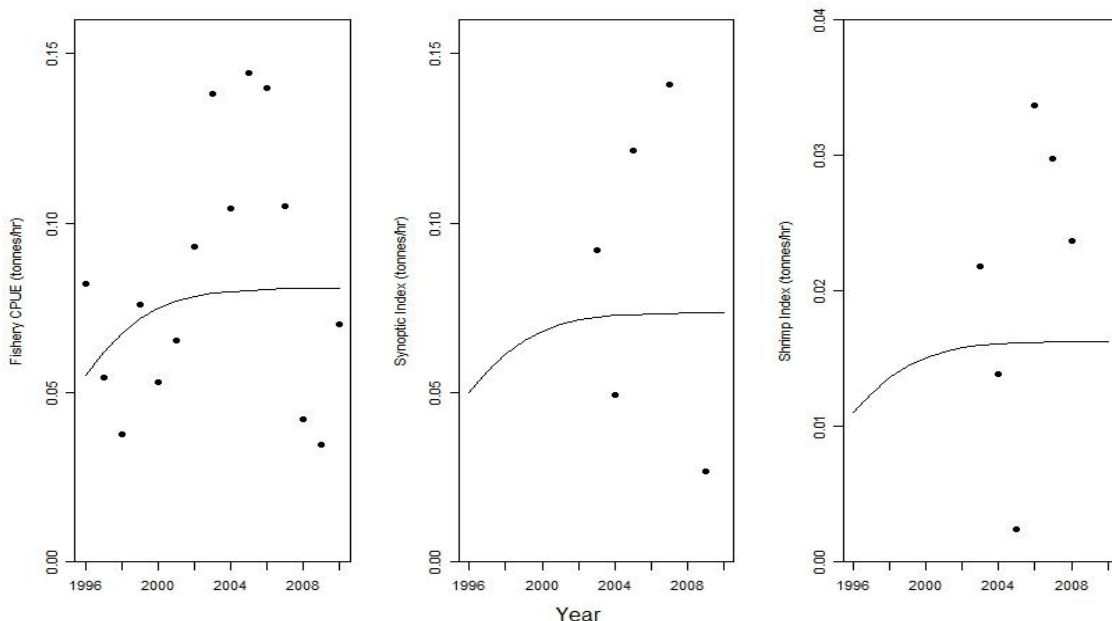


**Figure 21.** Posterior distribution of the instantaneous fishing mortality that results in  $MSY$ ,  $F_{MSY}$ , for QCS (solid line) and NHS (dashed line) stocks.

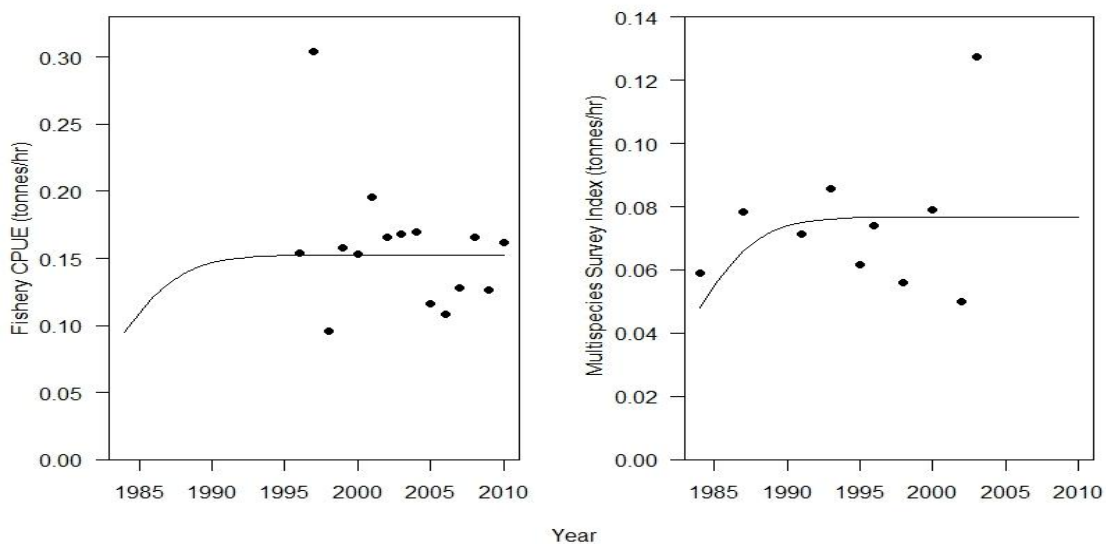


**Figure 22.** The log predicted big skate population abundance in QCS (left) from 1996-2010 and NHS (right) from 1984-2010. The light grey is the 90% quantile, medium grey is the 80% quantile, dark grey is the 50% quantile and the solid black line is the median predicted population biomass.





**Figure 23.** Observed and predicted indices of abundance for the QCS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters. Fishery CPUE is shown on the left figure, QCS Synoptic Survey in the middle, and QCS Shrimp Survey on the right.



**Figure 24.** Observed and predicted indices of abundance for the NHS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters. Fishery CPUE is shown on the left and the Hecate Strait Multispecies Survey on the right.

**Table 3.** Statistics from the posterior distribution of the three parameters of the Graham-Schaefer biomass dynamics model for Queen Charlotte Sound.

Parameter	2.50%	25%	Median	75%	97.50%	Mean	SD
$r$ (year <sup>-1</sup> )	0.285	0.342	0.385	0.441	0.579	0.397	0.076
K (tonnes)	10,963	129,080	698,266	2,718,540	8,222,520	1,836,096	2,379,094
depletion	0.332	0.542	0.680	0.824	0.980	0.678	0.181

**Table 4.** Statistics from the posterior distribution of the three parameters of the Graham-Schaefer biomass dynamics model for North Hecate Strait.

Parameter	2.50%	25%	Median	75%	97.50%	Mean	SD
$r$ (year <sup>-1</sup> )	0.283	0.343	0.391	0.450	0.578	0.402	0.077
K (tonnes)	6,594	76,652	501,174	2,385,481	8,587,588	1,650,477	2,340,178
depletion	0.091	0.399	0.624	0.808	0.980	0.597	0.256

**Table 5.** Statistics for the management parameters calculated using the posterior distributions of the three parameters of the Graham-Schaefer biomass dynamics model for Queen Charlotte Sound.

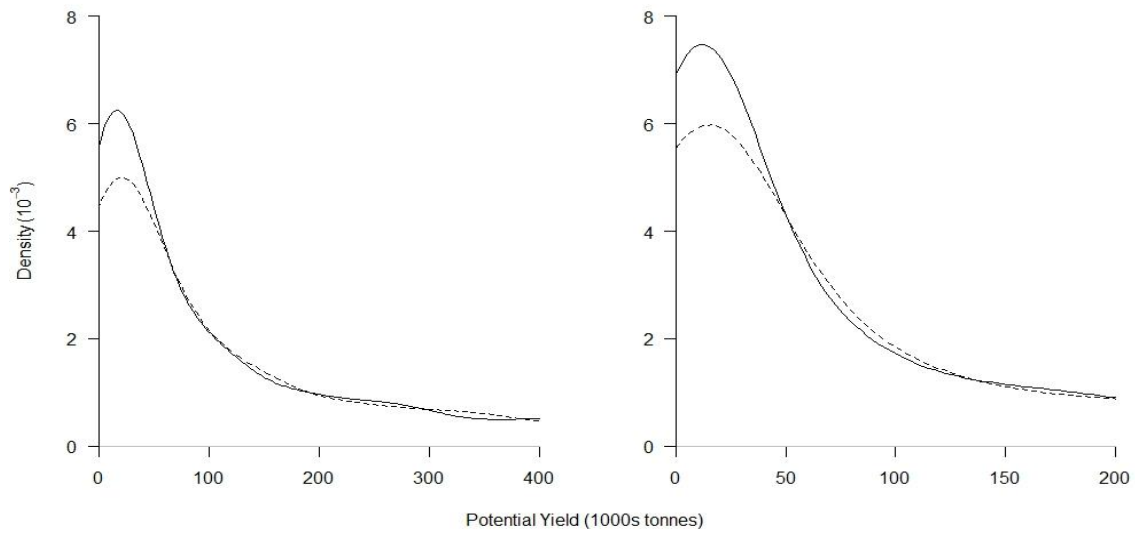
Management Target	2.50%	25%	Median	75%	97.50%	Mean	SD
MSY (tonnes)	1,082	12,426	67,706	264,363	822,354	181,187	239,500
$B_{msy}$ (tonnes)	5,481	64,540	349,133	1,359,270	4,111,260	918,048	1,189,547
$F_{msy}$	0.142	0.171	0.192	0.220	0.290	0.198	0.037

**Table 6.** Statistics for the management parameters calculated using the posterior distributions of the three parameters of the Graham-Schaefer biomass dynamics model for North Hecate Strait.

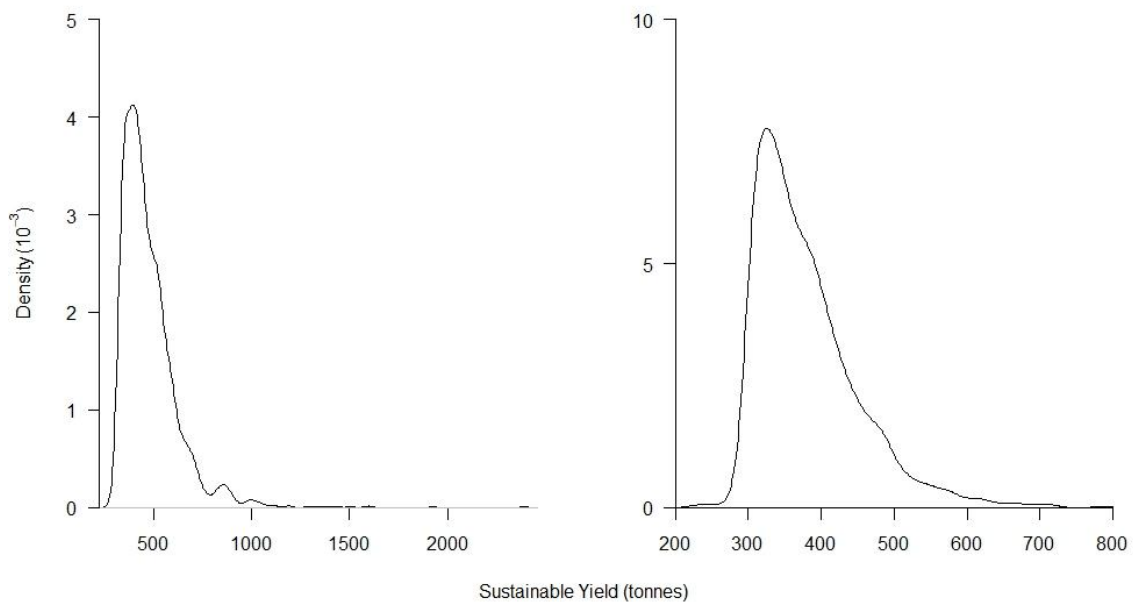
Management Target	2.50%	25%	Median	75%	97.50%	Mean	SD
MSY (tonnes)	695	7,349	49,141	231,397	871,076	166,095	242,348
$B_{msy}$ (tonnes)	3,297	38,326	250,587	1,192,740	4,293,794	825,238	1,170,089
$F_{msy}$	0.141	0.171	0.196	0.225	0.289	0.201	0.039

### 3.3 Depletion-Corrected Average Catch Analysis

DCAC estimates of potential yield ( $Y_{pot}$ ) for each stock were lower than the  $MSY$  values estimated using the BDMs due to DCAC's assumption of  $B_{MSY}$  occurring at 40% of  $B_0$  rather than 50% of  $B_0$ . Resulting estimates of sustainable yield ( $Y_{sust}$ ) were significantly lower than both the  $Y_{pot}$  and  $MSY$  because both stocks are estimated to be well above  $B_{MSY}$ . If the stocks were at  $B_{MSY}$  then they would be able to sustain removals equal to  $Y_{pot}$ ; the mode of the  $Y_{pot}$  posteriors were estimated at 17,500 tonnes and 13,000 tonnes for QCS and NHS, respectively (Figure 25). According to the mode of the  $Y_{sust}$  posteriors, QCS and NHS stocks can sustain removals of 370 and 330 tonnes, respectively, without changing the current estimated stock size (Figure 26). The current TAC on NHS, equal to 567 tonnes, is lower than the maximum  $Y_{sust}$  predicted by DCAC (approximately 850 tonnes). Given the assumed range of  $\Delta$  values, the range of predicted  $Y_{sust}$  for QCS was 300-2,400 tonnes and 225-850 tonnes for NHS. The lower  $Y_{sust}$  values for NHS compared to QCS may be a result of my zero catch assumption from 1984-1995 for NHS. Also, lower  $Y_{sust}$  values for NHS may be due to the higher, positive  $\Delta$  values predicted by the BDM for NHS (0.66 versus 0.11 for QCS). The relatively low  $Y_{sust}$  values occur because the current predicted abundance in each stock is near or at carrying capacity and thus experiencing strong effects of density-dependence. Tables 7 and 8 show the 2.5, 25, 50, 75, and 97.5% quantiles, mean, and standard deviation for  $Y_{pot}$  and  $Y_{sust}$ , respectively.



**Figure 25.** Potential yield ( $Y_{pot}$ ) (solid line) calculated through DCAC compared to MSY (dashed line) estimated from the Graham-Schaefer BDM for QCS (left) and NHS (right).



**Figure 26.** Sustainable yield ( $Y_{sust}$ ) distribution calculated using DCAC for the QCS (left) and NHS (right) stocks.

**Table 7.** Statistics for the potential and sustainable yield distributions for the QCS stock of big skate calculated using DCAC methods.

Management Target	2.50%	25%	Median	75%	97.50%	Mean	SD
$Y_{pot}$	866	9,940	54,165	211,490	657,883	144,950	191,600
$Y_{sust}$	327	382	442	533	865	480	154

**Table 8.** Statistics for the potential and sustainable yield distributions for the NHS stock of big skate calculated using DCAC methods.

Management Target	2.50%	25%	Median	75%	97.50%	Mean	SD
$Y_{pot}$	843	10,366	54,031	215,090	685,603	147,598	196,598
$Y_{sust}$	300	325	359	411	568	379	73

### 3.4 Sensitivity Analyses on Discard Mortality Rate

The 0 and 100% discard mortality rates mainly affected the output produced by DCAC. The DCAC sustainable yield increased for both stocks with an increasing discard mortality rate (Tables 9 and 10). Sustainable yield increased with increasing discard mortality rate because the total catch increases when the model assumes more skate are dead post-capture. A higher historical total catch increases the numerator in the sustainable yield equation thus producing a larger sustainable yield. The QCS stock showed increasing  $K$ ,  $MSY$ , and  $B_{MSY}$  with increasing discard mortality rates but trends for NHS were less clear. Discard mortality rates did not affect the overall shape of the parameter posterior distributions likely because discards were low relative to overall catch (Appendix I and II).

**Table 9.** Modes of posterior probability distributions for QCS under the three discard mortality rate scenarios.

	0%	50%	100%
r (year <sup>-1</sup> )	0.374	0.366	0.367
K (tonnes)	190,006	202,184	214,879
depletion	0.716	0.720	0.597
MSY (tonnes)	19,579	21,831	22,338
B <sub>msy</sub> (tonnes)	95,003	101,092	107,439
F <sub>msy</sub>	0.187	0.183	0.184
Y <sub>pot</sub>	15,663	17,464	17,871
Y <sub>sust</sub>	346	365	388

**Table 10.** Modes of posterior probability distributions for NHS under the three discard mortality rate scenarios.

	0%	50%	100%
r (year <sup>-1</sup> )	0.367	0.359	0.361
K (tonnes)	136,358	158,603	172,482
depletion	0.743	0.789	0.749
MSY (tonnes)	14,732	16,196	15,655
B <sub>msy</sub> (tonnes)	68,179	79,302	86,241
F <sub>msy</sub>	0.184	0.179	0.180
Y <sub>pot</sub>	11,786	12,957	12,524
Y <sub>sust</sub>	290	325	365

## 4: DISCUSSION

The biomass dynamics models (BDMs) for Queen Charlotte Sound (QCS) and North Hecate Strait (NHS) predict both stocks to be stable at their respective carrying capacities given the available data. However, the population abundance estimates and their relationship to carrying capacity are uncertain since CPUE and survey indices lacked the variation needed to reliably fit a BDM. The BDMs predict maximum sustainable yields ( $MSY$ ) of 21,800 and 16,200 tonnes.

Depletion-corrected average catch (DCAC) analysis predicts that if the population is to remain at its current abundance, 370 and 330 tonnes may be removed sustainably ( $Y_{sust}$ ) from QCS and NHS, respectively. If the stocks were at the biomass that supports  $MSY$  ( $B_{MSY}$ ) they could support removals equal to  $MSY$ , or, if managers wish to be more conservative, equal to the potential yield calculated by DCAC (16,500 and 13,000 tonnes for QCS and NHS). However, because the models predict both stocks to be at carrying capacity they are not as productive as they would be if at  $B_{MSY}$ . The following sections discuss how the uncertainty in available life history and fishery data affect model outcomes. I follow with applications of my stock assessment results to potential management objectives and summarize with conclusions.

#### 4.1 Bayesian Approach to Estimate $r_{max}$ from a Growth Curve

The female length-at-age data used to fit the von Bertalanffy growth function (VBGF) created difficulties for parameter estimation. The available length-at-age data did not reach an asymptote within the observed range of lengths. Consequently, the data contained little information on the true value of  $L_{\infty}$  as evidenced by the similar shapes of the prior and posterior probability distributions. The mean and median posterior estimates of  $L_{\infty}$  were higher than the estimated  $L_{\infty}$  for female big skate in the Gulf of Alaska (GOA) (Gburski et al., 2007). The difference in  $L_{\infty}$  is not surprising given that no big skates larger than 1780 mm were observed in the GOA study whereas skates as large as 2040 mm have been observed in BC. The median of the posterior distribution of  $k$ , the growth rate of the VBGF, was approximately half the  $k$  estimated for GOA big skate,  $0.0796 \text{ year}^{-1}$  (Gburski et al., 2007). Estimates of  $k$  for big skate calculated using life history invariant equations equalled  $0.10\text{-}0.14 \text{ year}^{-1}$  (Benson et al., 2001). The re-capture and ageing of larger (and older) female big skate would greatly improve the data set used to fit the VBGF and subsequent parameter estimations.

Natural mortality ( $M$ ) is vital for inputs to stock assessments but it is also one of the most difficult parameters to calculate directly, hence it is usually calculated indirectly from a growth curve using life history invariant theory (Hewitt and Hoenig, 2005). The width of  $L_{\infty}$  and  $k$  posterior distributions resulted in a wide range of possible  $M$  values. However, the resulting distribution of  $M$  accounts for uncertainty in both the life history parameters and model coefficients



used in its calculation. My research produced model estimates of  $M$  similar to those of the roughskin skate (*Dipturus trachyderma*) which grows to similar sizes as the big skate and has an estimated mean  $M$  between 0.089-0.184 year<sup>-1</sup> (Quiroz et al., 2010). Researchers estimate maximum age of big skate to be approximately 26 years which results in a natural mortality of 1/26, or 0.038 year<sup>-1</sup>, based on life history theory (King and McFarlane, 2010). Big skate natural mortality estimated from a predictive equation based on data from numerous fish stocks is larger than the median and mean estimated in my assessment (0.162 year<sup>-1</sup> versus 0.037 and 0.047 year<sup>-1</sup>; Hoenig, 1983; Hewitt and Hoenig, 2005). However, the oldest observed skate likely underestimates the true maximum age and the larger estimate based on the predictive equation is still within the range of possible  $M$  values calculated in my model. I recommend an alternate method of calculating natural mortality (e.g., Hoenig and Hewitt, 2005) given the uncertainty present in the estimates of  $L_{\infty}$  and  $k$ , until more data becomes available.

The probability distribution of  $r_{max}$  incorporated all possible sources of uncertainty in the form of probability distributions for the life history parameters used in its calculation: asymptotic maximum length ( $L_{\infty}$ ), growth rate ( $k$ ), age at maturity ( $\alpha$ ), breeding interval ( $i$ ), and litter size ( $l$ ). A previous estimate of potential rate of population increase ( $r'=0.26$  year<sup>-1</sup>, Benson et al., 2001), calculated using female maximum length ( $L_{max}=1680$  mm), is smaller than the mean  $r_{max}$  estimated in this research. However, the  $r_{max}$  calculated in my research considered other life history parameters, such as litter size and breeding interval,

which may attribute to the larger mean  $r_{max}$  (Benson et al., 2001; Frisk et al., 2001). Through the sensitivity analysis of age at selectivity on  $r_{max}$ , I found that as the age of selectivity to the fishery approaches the age of maturation, the Euler-Lotka model predicts a larger mean and range for  $r_{max}$  (Myers and Mertz, 1998). Therefore, if the actual age of selectivity of big skate is larger than one, the resulting distribution of  $r_{max}$  may not be as informative as the distribution produced in the current assessment. In order to facilitate the calculation of selectivity curves for big skate, onboard observers should collect length data on trawl tows that target big skate whenever possible.

#### **4.2 Uncertainty in Management Parameter and Abundance Estimation using BDMs and DCAC**

Posterior distributions for  $r$ ,  $K$ , and *depletion* for QCS and NHS were highly dependent on the informative prior probability distribution used for  $r$ . Due to the lack of variation in the CPUE and survey data, the prior probability distribution of  $r$  outweighs the likelihood of the data resulting in a posterior distribution for  $r$  that identically matches its prior distribution. The informative prior for  $r$  influences the posterior distribution for  $K$  since these two parameters are inversely correlated (Hilborn and Walters, 1992). In order to get reliable estimates of  $K$ , fishery data needs to have contrast. Ideally, data should be collected from when the population is near  $K$  (i.e., pre-exploitation), when it has been fished to low abundances, and then when it is allowed to recover. Furthermore, the informative prior for  $r$  also indirectly affects the posterior distribution of depletion since it is calculated jointly with  $r$  and  $K$ .

The extent of uncertainty in estimates of  $MSY$ ,  $B_{MSY}$  and  $F_{MSY}$  are directly related to the uncertainty in the estimates of  $r$  and  $K$ . The high uncertainty in the estimates of  $MSY$  is due in part to the high uncertainty in  $K$  while estimates of  $B_{MSY}$  are entirely dependent on the uncertainty of the  $K$  posterior. The tight distribution of the  $F_{MSY}$  posteriors are a function of the informative priors and tight posterior distributions for  $r$ . For elasmobranchs,  $MSY$  generally ranges between 4.5 and 7.5% of the unexploited biomass (Anderson, 1990). The  $MSY$  was estimated between 6.5 and 7.6% of the unexploited biomass in a multispecies ray fishery in the South Atlantic (Agnew et al., 2000). I found the mode of the  $MSY$  posterior to be approximately 10% of the mode of the  $K$  posterior in both QCS and NHS (21,800/202,000 tonnes for QCS and 16,200/159,000 tonnes for NHS). It is likely that creating an informative prior for  $K$ , possibly by using density estimates for big skate and area swept data from research surveys, would narrow the range of possible  $MSY$  and  $B_{MSY}$  values.

The median predicted population size and predicted indices of abundance of big skate in each stock were stable during the later part of the time series. The wide range of predicted population sizes results from the skewed  $K$  posterior distribution. As previously mentioned, creating an informative prior for  $K$  could generate a narrower range of predicted population abundances. The model output suggests that the catch taken from 1996-2010 did not have a significant effect on the population dynamics of big skate in either stock. The best fit to the multiple indices of abundance used in my assessment was a relatively horizontal line through the later data points in the time series and was likely due to the

variability and lack of contrast in the data. It is unknown if the lack of trends observed in the data are representative of the true population abundance.

The DCAC potential yield is a conservative estimate of  $MSY$  while the DCAC sustainable yield calculates the yield that can be removed from the stock while maintaining the stock at its current abundance (MacCall, 2009). The potential yield was slightly lower than the  $MSY$  estimated from the BDMs because the potential yield equation assumes  $B_{MSY}$  occurs at 40% of  $B_0$  whereas the Graham-Schaefer assumes  $B_{MSY}$  occurs at 50% of  $B_0$ . I recommend using the potential yield in lieu of  $MSY$  as  $B_{MSY}$  for elasmobranchs is believed to occur between 35-48% of unfished biomass (Anderson, 1990). The DCAC sustainable yield is significantly lower than the potential yield and  $MSY$  because both stocks are estimated to be at carrying capacity. A stock at carrying capacity is not as productive as a stock below carrying capacity due to the strong effects of density-dependence resulting in low birth rates relative to death rates. The BDMs predicted an increase in both stock's biomass since the beginning of their respective time series; hence, most of the depletion ( $\Delta$ ) values assumed were negative and the resulting modal sustainable yields predicted (370 and 330 tonnes for QCS and NHS) are larger than the average of historic catches (323 and 301 tonnes for QCS and NHS).

### **4.3 Management Applications**

A harvest strategy for the big skate fishery in British Columbia requires clear management objectives from DFO. There is currently a total allowable catch (TAC) of 567 tonnes in NHS, but there is no TAC for big skate in QCS

(DFO, 2011). The TAC encompasses both landings and estimated discards in the trawl sector of the fishery (DFO, 2011). In accordance with DFO's goal to adhere to the precautionary approach, all management advice needs to account for uncertainty while taking action to avoid harm to stocks and the ecosystem (DFO, 2006). DFO incorporates the precautionary approach into their stock assessments by defining three zones that describe stock status: healthy, cautious, and critical (DFO, 2006). The lower limit reference point (LRP) divides the critical zone from the cautious zone (DFO, 2006). Below the LRP, the stock is in the critical zone, the removal rate (usually expressed in terms of fishing mortality) approaches zero, and efforts to promote stock re-building are initiated. The upper stock reference (USR) divides the cautious zone from the healthy zone (DFO, 2006). Below the USR, the stock is in the cautious zone and the removal rate from the stock is reduced accordingly in order to avoid reaching the LRP. Above the USR, the stock is in the healthy zone. Therefore, a target reference point (TRP), a desirable target for management, should be above the USR to maintain the stock in the healthy zone. Ultimately, the harvest rate chosen depends on the zone in which the stock lies. For example, if the stock is in the cautious zone harvest rates are set so that the stock rebuilds into the healthy zone (DFO, 2006). DFO's Sustainable Fishery Framework states that DFO's goal is to keep stocks in the healthy zone and out of the critical zone (DFO, 2011). I will outline two potential DFO management goals, their accompanying management advice based on the results of this assessment, and discuss data collection routines to improve future management advice.

The first potential DFO management goal may be to maintain big skate abundance at current levels. I estimated that both stocks are near or at carrying capacity, thus experiencing relatively low productivity due to density dependence. Hence, the only way to maintain current stock size and the resultant low productivity is through relatively low removals. Big skate catch increased by 245% since 2008 in QCS and by 72% since 2007 in NHS, yet both stocks continue to be near their respective carrying capacities. According to my assessment, both big skate stocks have remained relatively stable even with the current catches and the relatively high catch taken in both stocks in 2003. My study shows that the catches experienced during the time series available had little effect on big skate population dynamics. If big skate catches from QCS and NHS remain within the range of past catches then DFO will be able to maintain the current big skate abundance without having to establish a TAC. DFO should continue to monitor catches, continue to track population trends through fishery-independent surveys, and reassess population status in a few years or earlier if there is a dramatically large increase in catches.

DFO fishery managers may be interested in more conservative skate management considering the declines of skate species in global fisheries (Brander, 1981; Casey and Myers, 1998; Walker and Hislop, 1998; Dulvy et al., 2000) coupled with the possibility of increased skate catch in BC to supply global demand. To do this, managers can set a TAC in QCS equal to the largest predicted DCAC sustainable yield (2,400 tonnes) and in NHS equal to the highest catch from the time series (approximately 1,000 tonnes). I do not

recommend managers use the DCAC sustainable yield predicted for NHS because my assumption of zero catch from 1984-1995 had a significant effect on the calculated average catch. Average catch from 1984-2010 is 301 tonnes (=8,140 tonnes/27 years) but average catch from 1996-2010 is 542 tonnes (=8,140 tonnes/15 years). Had I only used catch data from 1996-2010 or assumed non-zero catch from 1984-1995, the resulting sustainable yield estimates would be larger than those presented in this assessment. Zero big skate catch from 1984-1995 is unlikely because, although not targeted prior to 1996, they were likely caught and discarded in trawl fisheries (Benson et al., 2001). Once the TAC for big skate is met in either stock, fishing for big skate would cease in that location. Since big skate are caught alongside other commercially important species, such as Pacific cod, setting a TAC for big skate would potentially impact fisheries for other species.

Like most tactics used to regulate fisheries, TACs have advantages and disadvantages. An output control, such as a TAC, has the benefit of regulating how much catch is taken as opposed to using an input control, such as fixed season length, which cannot control for effort. Additionally, input controls (e.g., a limit on the number of trips taken) are harder to decrease in a fishery and can lead to increases in effort through other mechanisms such as increases in fishing power through technical means (Beddington et al., 2007). Two of the main disadvantages of TACs are that they require a large amount of data and are expensive to implement because of monitoring and enforcement (Hilborn and Walters, 1992). However, monitoring and enforcement costs are already borne

by DFO and the fishery so the marginal cost will be small compared to the benefits of monitoring catch and a lower risk of moving into an undesirable stock status zone. Another important disadvantage in using TACs is that they assume stock size is well known. If stock size is over-estimated, the TAC put in place may actually be too high, driving the stock abundance down. The effect of over-estimating a TAC will have prolonged effects on future stock sizes and catches (Hilborn and Walters, 1992). Conversely, if the stock size is under-estimated, the TAC will also be underestimated and managers will unknowingly forego potential profit. Choosing a TAC for the big skate stocks may be difficult given the information available.

DFO's second potential management goal could be to maximize the productivity and profitability of the big skate fishery. Given that my study estimates both stocks to be at carrying capacity, each stock would first need to be fished down to its  $B_{MSY}$ , which under logistic growth assumptions is approximately half a stock's carrying capacity. Since big skate catches are driven by market demand, establishing a higher TAC may not be enough to decrease the stocks to  $B_{MSY}$ . The established TAC in NHS does not seem to limit the fishery as evidenced by the low catches relative to the 567 tonnes TAC (excluding 2003). Additionally, catches in QCS have not exceeded 1,000 tonnes even though there is no TAC present on big skate catch in that stock. Based on the big skate catch trajectory it seems that there are other factors influencing why, when, and how much fishers target and land big skate. Managers can employ incentives, such as priority access to increased quota for other target



species, to motivate fishers to target and catch big skate. Once stocks are reduced to  $B_{MSY}$  they are more productive than a stock at carrying capacity and can support removals equal to  $MSY$ . Managers can introduce a Limited Access Program (LAP) to limit vessel numbers in order to avoid overcapitalization, thus ensuring increased profits for those active in the fishery (Quigley, 2006). Managers can use adaptive management and decision analysis to determine the incentive program that is most likely to reduce big skate abundance and increase profitability.

Adaptive management is an iterative process by which a management regulation is enforced, the outcome is monitored, and the current management regulation is updated using the knowledge gained (Lee, 1999). Adaptive management treats policy decisions as large-scale experiments. These experiments provide a way to learn about dynamic, complicated systems and can potentially improve management (Walters, 2007). Decision analysis, recommended for use in shark stock assessments (McAllister et al., 2001), could be used by DFO managers to select an incentive program to motivate fishers to reduce big skate abundance. A decision analysis would require the alternative uncertain states of nature, the probability of each uncertain state occurring, and decision tables to determine the probability of each outcome (McAllister et al., 1994). For BC's big skate fishery, the potential management decisions are different incentive programs to get fishers to target big skate. The uncertain states of nature are the  $r$  and  $K$  parameters from the biomass dynamics model, which dictate predicted population size, the predicted response of the fishers to

the incentive program, and the catch resulting from the incentive program chosen. The probabilities associated with each value of  $r$  and  $K$  can be taken directly from the posterior probability distributions generated from the biomass dynamics model used in this assessment. The predicted response of fishers to an incentive program and the resulting catch can be determined by fisher preference surveys and interviews as some incentives may be more attractive than others. Incentives deemed more attractive by fishers may be more effective at reducing the population to the desired abundance. Multiple outcomes are possible from the decision analysis such as the time it would take to fish the stock down to  $B_{MSY}$ , the revenue generated from the catch level resulting from a particular incentive program, and/or the cost of the incentive program. Managers can apply the results from the decision analysis in an adaptive management approach to one stock (the experimental unit) while keeping the other stock as a control. The principal benefit of an adaptive management approach is the ability to empirically reduce the uncertainty inherent in fisheries management by undertaking experiments and updating existing knowledge (Botsford et al., 1997). Adaptive management can be costly in terms of time and money when a suitable solution is not found (Lee, 1999). However, adaptive management provides a long-term plan and the opportunity to learn about system responses to management as opposed to establishing a quota and monitoring outcomes.

Data collection and monitoring is an on-going and pivotal part of the management process regardless of management objectives. Data collection and monitoring can determine the efficacy of current management regulations. Data

collection in the form of a depletion experiment can determine if research surveys (and fishery CPUE) are capturing true population trends (Hilborn and Walters, 1992). Additionally, depletion experiments in localized areas can give scientists and managers an estimate of abundance (Hilborn and Walters, 1992). To do this, I would recommend an experimental fishing-down of a portion of one stock while using the other as a control. If a portion of the experimental stock is depleted, one would expect to see a subsequent decrease in the CPUE and fishery-independent survey indices conducted in that stock. Survey procedures should measure relative abundance and use consistent gear and effort over time (Hilborn and Walters, 1992). After five years, the survey can be used along with fishery catches to determine initial and current stock sizes (Hilborn and Walters, 1992). Knowledge of current stock size can ensure that management regulations do not jeopardize stock status (i.e., move it into the cautious or critical zones). As onboard observers are already present on 100% of trawls in BC, length data on commercially caught big skate can provide information on size-selectivity to the fishery. Knowledge of size-selectivity is important because if fishers are targeting older, mature skates they may be reducing the reproductive potential of the population. Size-selectivity data could then be used to set minimum size limits on skate catch, if necessary, to reduce the chance of recruitment overfishing.

## 5: CONCLUSIONS

The model output presented here suggests that the two big skate stocks are unlikely to be overfished, as their estimated biomass is above the mode of their estimated  $B_{MSY}$ . If DFO's management goal is to maintain the current level of abundance in each stock, managers should monitor catches to ensure they are within the range of catches taken from 1996-2010. A TAC is not necessary since the historic catches do not seem to affect population dynamics according to my model. If fishery managers wish to be conservative, a TAC could be set to 2,400 tonnes for QCS based on the maximum predicted DCAC sustainable yield and 1,000 tonnes for NHS based on the highest catch from the time series available. If DFO's management goal is to increase the productivity and profitability of the big skate fishery, I would recommend a fishing down of the stocks to their  $B_{MSY}$ . An adaptive management approach can be taken on one of the two stocks to determine what incentive program motivates fishers to reduce stock abundance to  $B_{MSY}$  while also increasing profitability of the fishery. DFO should continue to collect data through depletion experiments and monitor stock status through trends in fishery-independent surveys. The research presented here provides fishery managers with results that incorporate uncertainty and can inform future management regulations for big skate in British Columbia.

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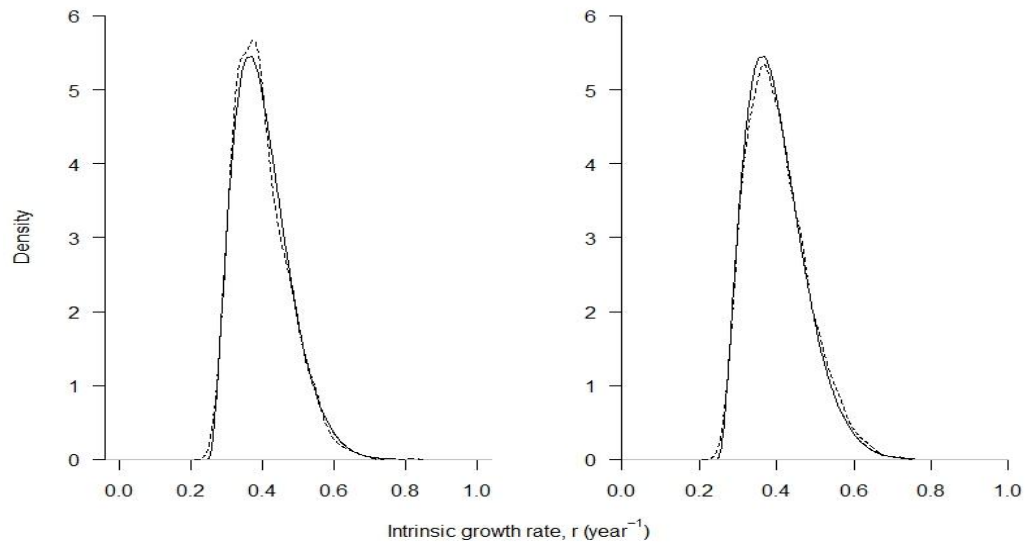
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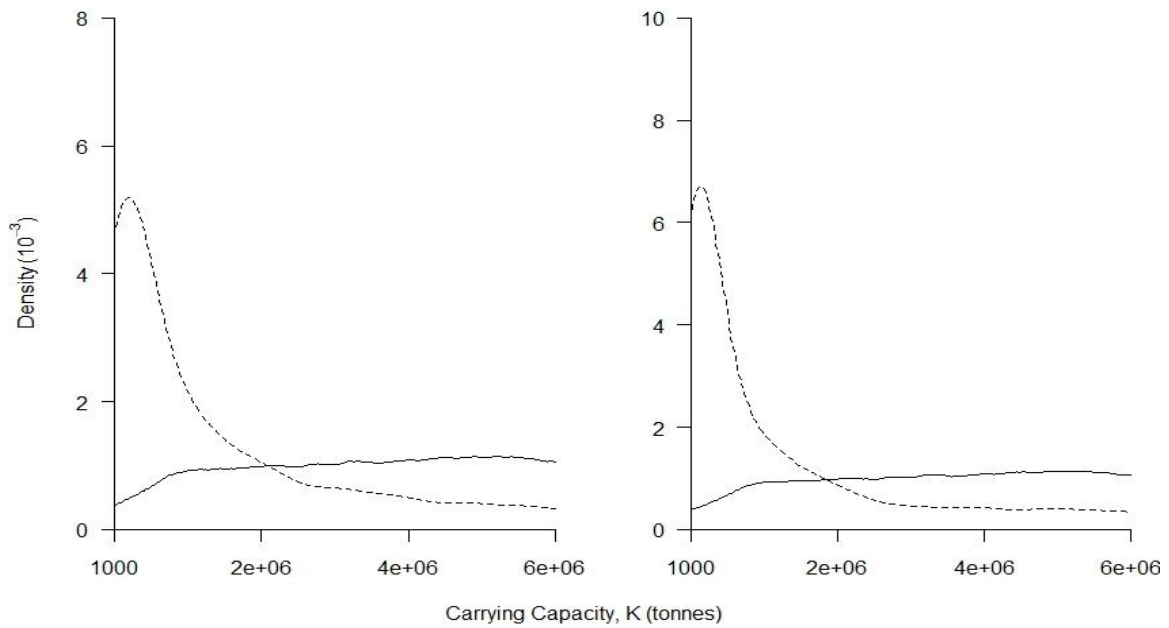
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# APPENDICES

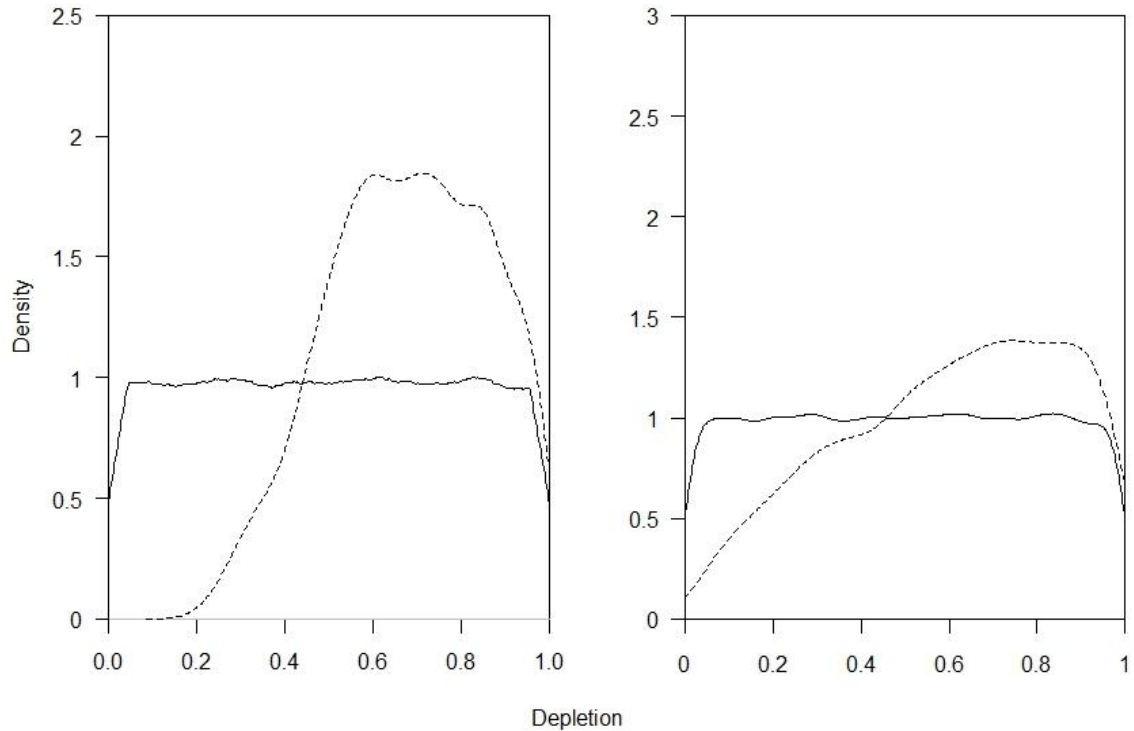
## Appendix 1: 0% Discard Mortality Rate Outputs



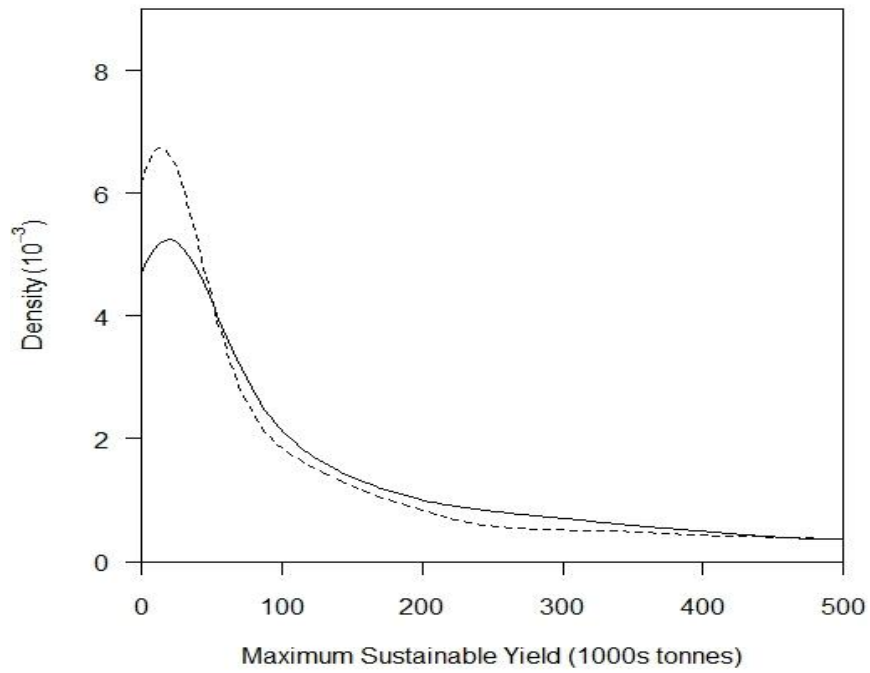
**Figure A1.1.** Prior (solid line) and posterior (dashed line) probability distributions for the intrinsic growth rate,  $r$ , from the QCS (left) and NHS (right) under a 0% discard mortality rate.



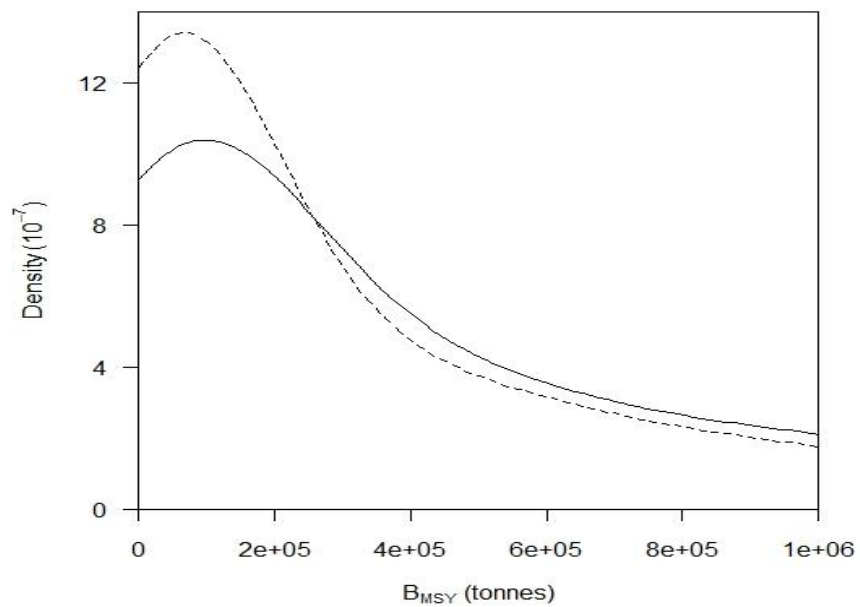
**Figure A1.2.** Prior (solid line) and posterior (dashed line) probability distributions of the carrying capacity,  $K$ , for the QCS (left) and NHS (right) under a 0% discard mortality rate.



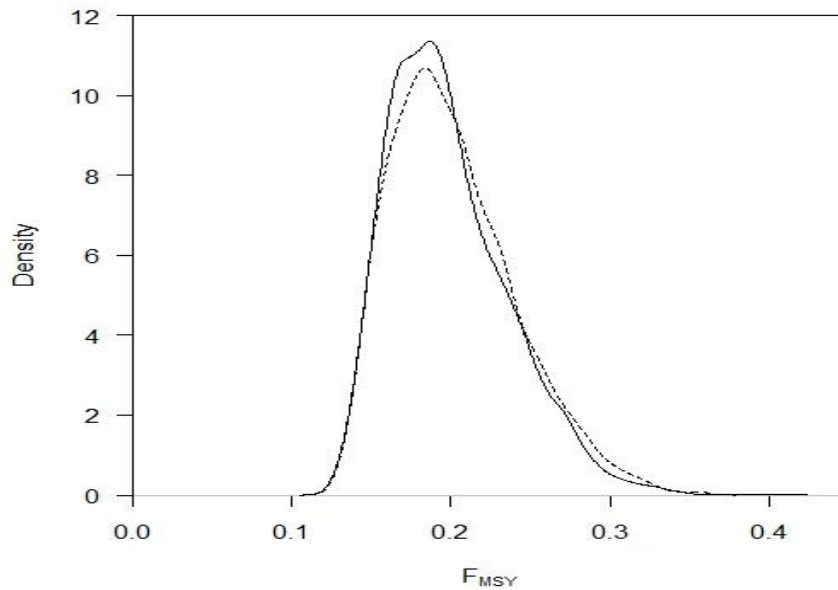
**Figure A1.3.** Prior (solid line) and posterior (dashed line) probability distributions for the depletion parameter of the QCS (left) and NHS (right) under a 0% discard mortality rate.



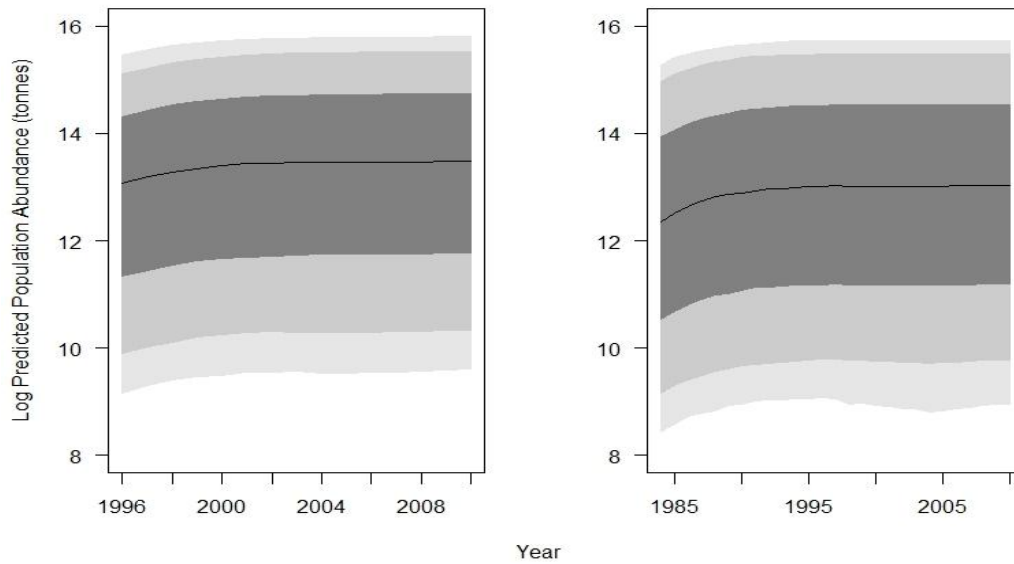
**Figure A1.4.**  $MSY$  posterior probability distribution for QCS (solid line) and NHS (dashed line) stocks measured in 1,000s of tonnes.



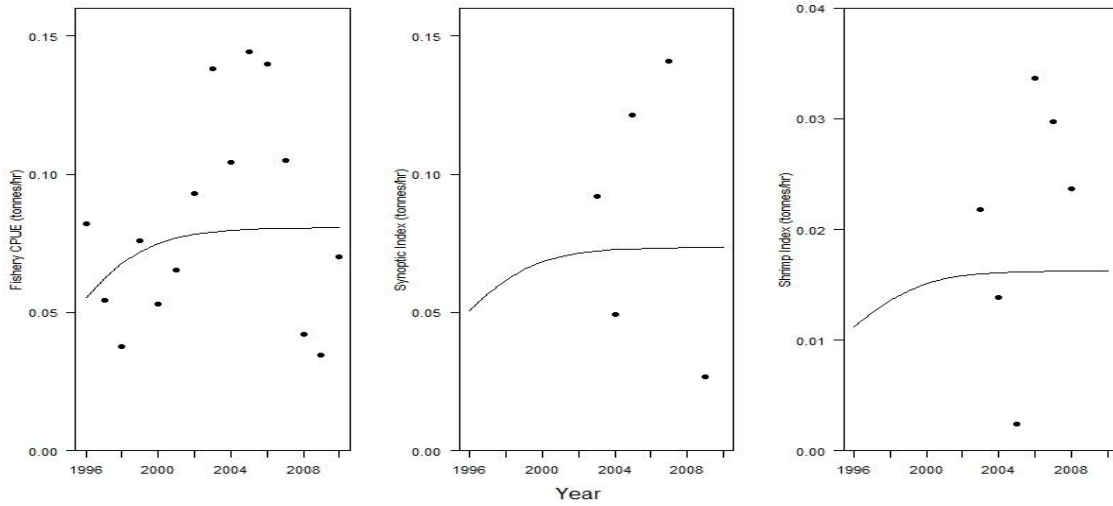
**Figure A1.5.**  $B_{MSY}$  posterior probability distribution for QCS (solid line) and NHS (dashed line) stocks measured in 1,000s of tonnes.



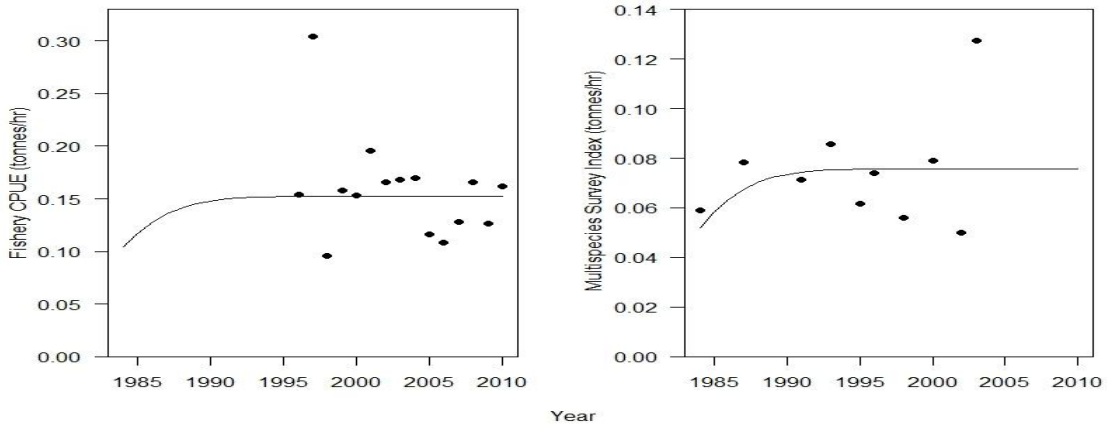
**Figure A1.6.** Posterior distribution of the instantaneous fishing mortality that results in  $MSY$ ,  $F_{MSY}$ , for QCS (solid line) and NHS (dashed line).



**Figure A1.7.** The log predicted big skate population abundance in QCS (left) from 1996-2010 and NHS (right) from 1984-2010. The light grey is the 90% quantile, medium grey is the 80% quantile, dark grey is the 50% quantile and the solid black line is the median predicted population biomass.

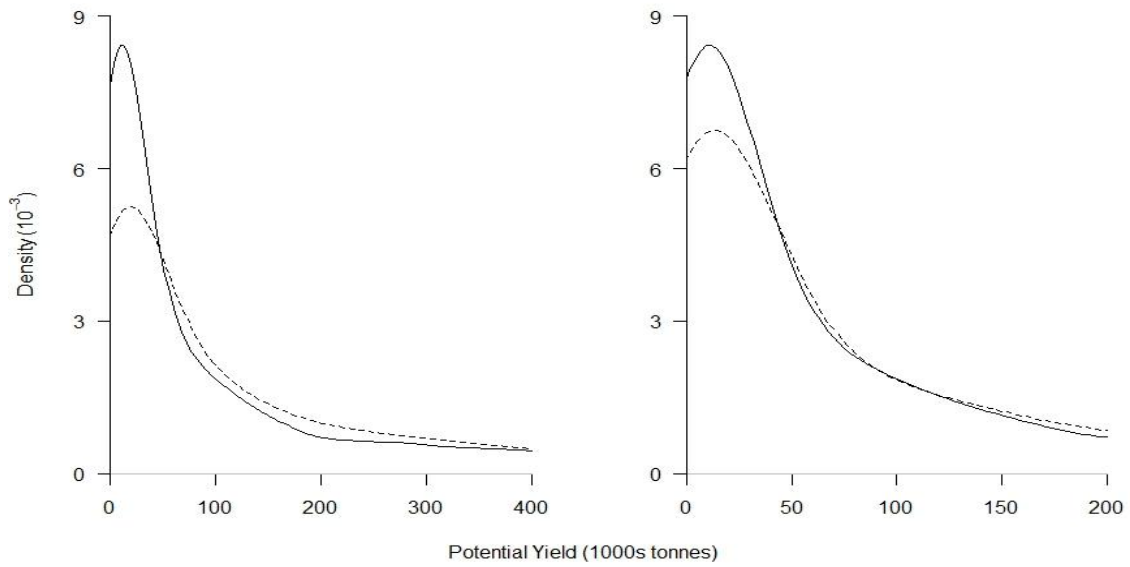


**Figure A1.8.** Observed and predicted indices of abundance for the QCS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters. Fishery CPUE is shown on the left figure, QCS Synoptic Survey in the middle, and QCS Shrimp Survey on the right.

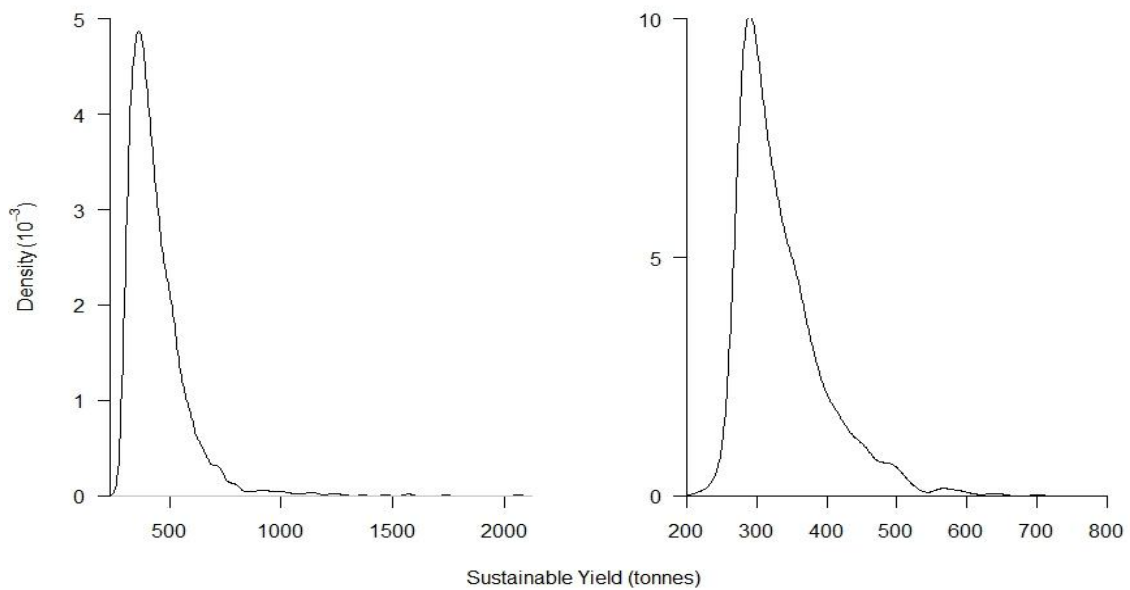


**Figure A1.9.** Observed and predicted indices of abundance for the NHS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters. Fishery CPUE is shown on the left and the Hecate Strait Multispecies Survey on the right.



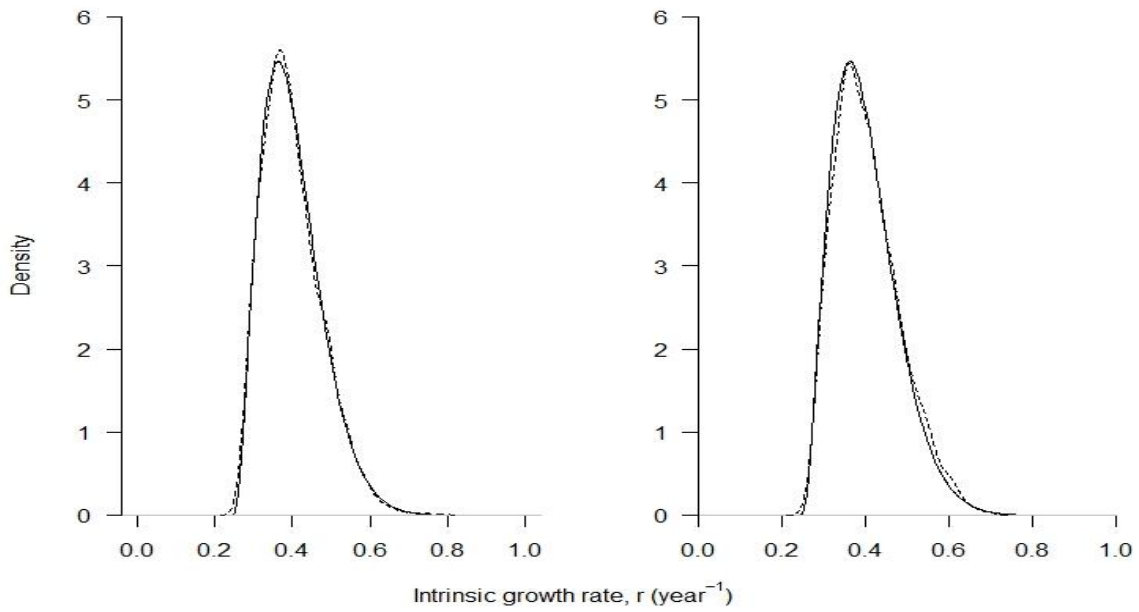


**Figure A1.10.** Potential yield (solid line) calculated through DCAC compared to MSY (dashed line) estimated from the Graham-Schaefer BDM for QCS (left) and NHS (right).

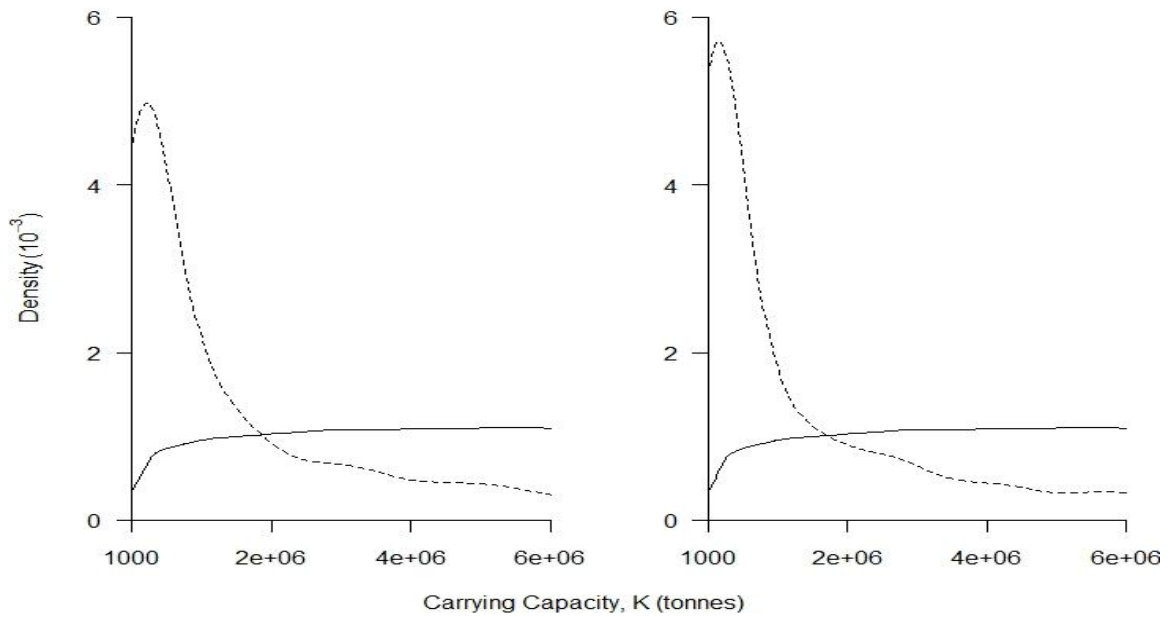


**Figure A1.11.** Sustainable yield distribution calculated using DCAC for the QCS (left) and NHS (right) stocks under a 0% discard mortality.

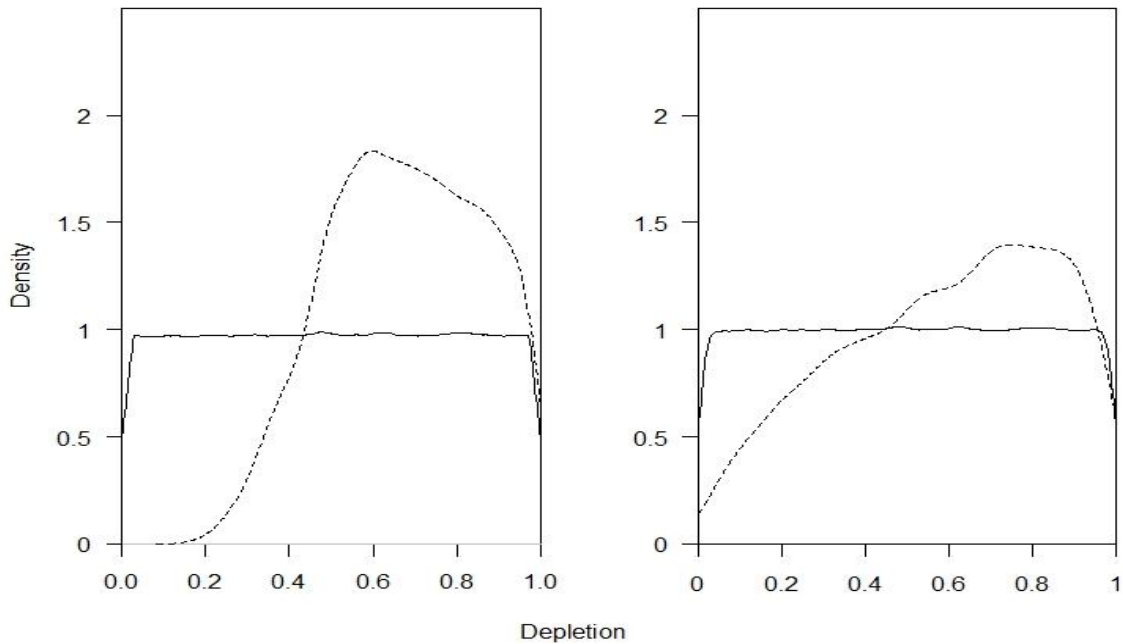
## Appendix 2: 100% Discard Mortality Rate Scenario



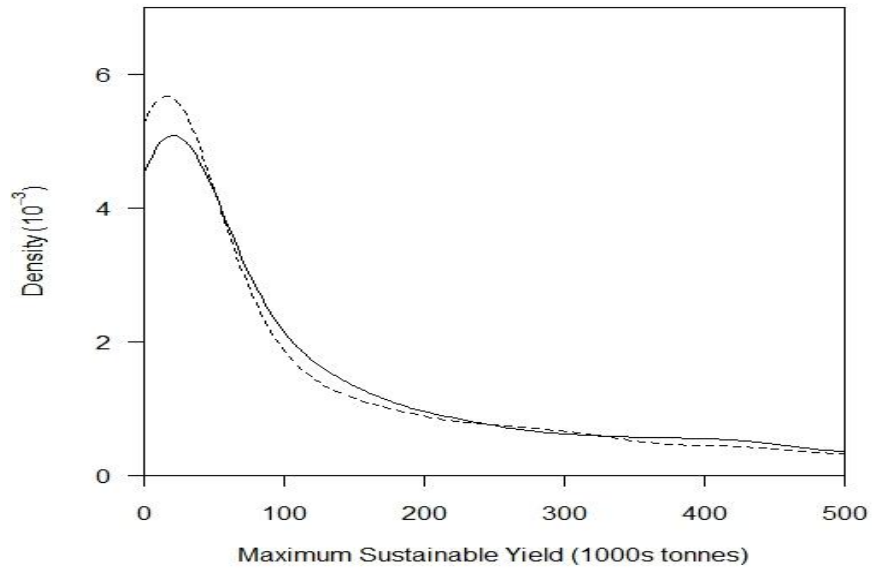
**Figure A2.1.** Prior (solid line) and posterior (dashed line) probability distributions for the intrinsic growth rate,  $r$ , from the QCS (left) and NHS (right) under a 100% discard mortality rate.



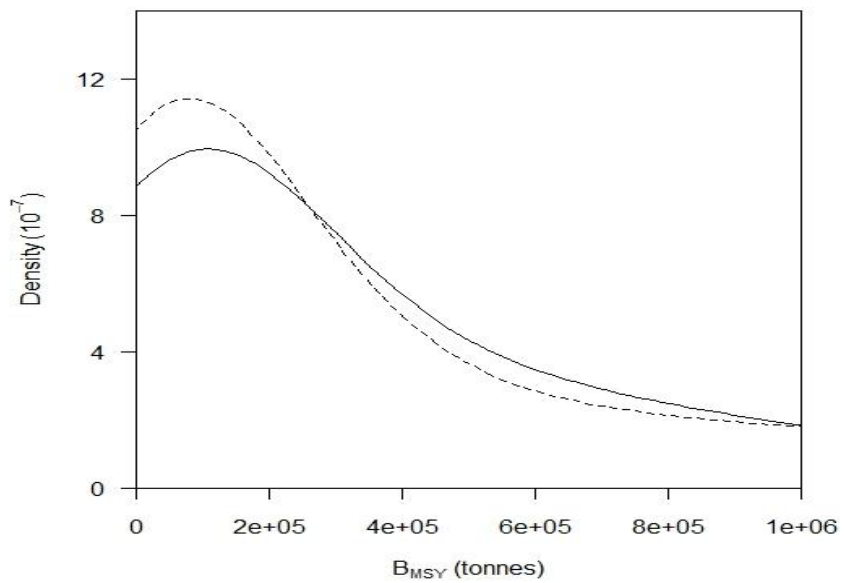
**Figure A2.2.** Prior (solid line) and posterior (dashed line) probability distributions of the carrying capacity,  $K$ , for the QCS (left) and NHS (right) under a 100% discard mortality rate.



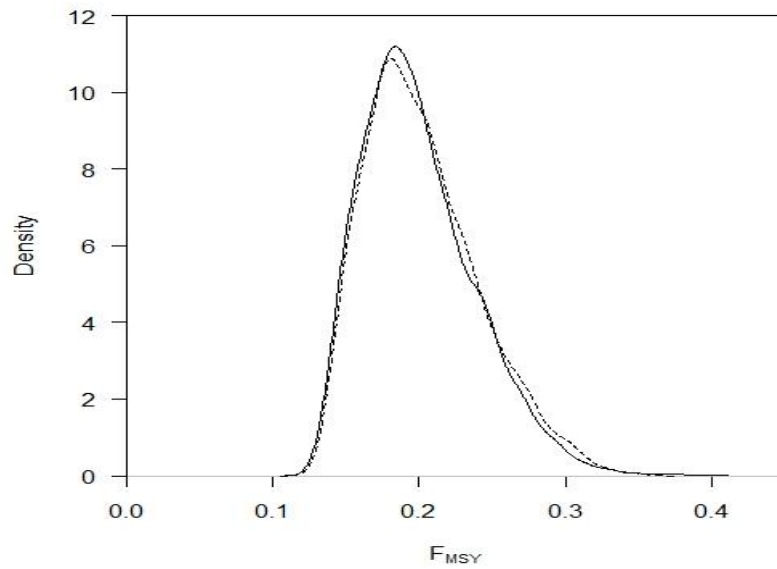
**Figure A2.3.** Prior (solid line) and posterior (dashed line) probability distributions for the depletion parameter of the QCS (left) and NHS (right) under a 100% discard mortality rate.



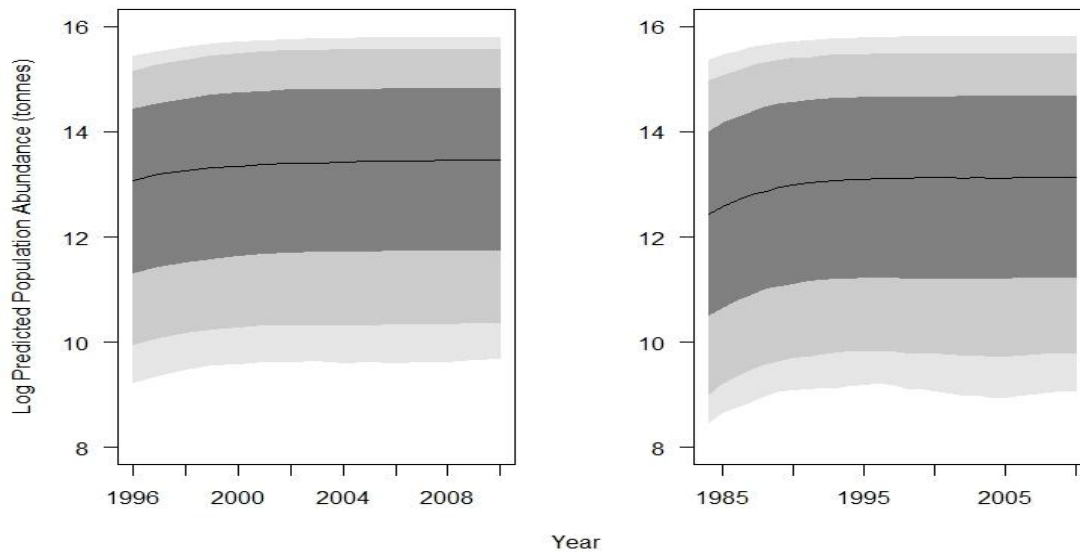
**Figure A2.4.**  $MSY$  posterior probability distribution for QCS (solid line) and NHS (dashed line) stocks measured in 1,000s of tonnes.



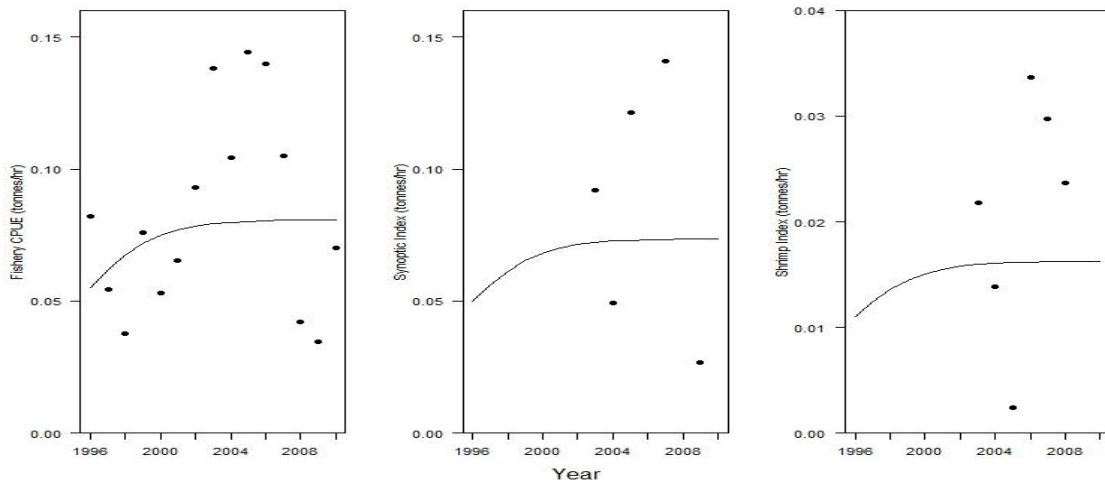
**Figure A2.5.**  $B_{MSY}$  posterior probability distribution for QCS (solid line) and NHS (dashed line) stocks measured in 1,000s of tonnes.



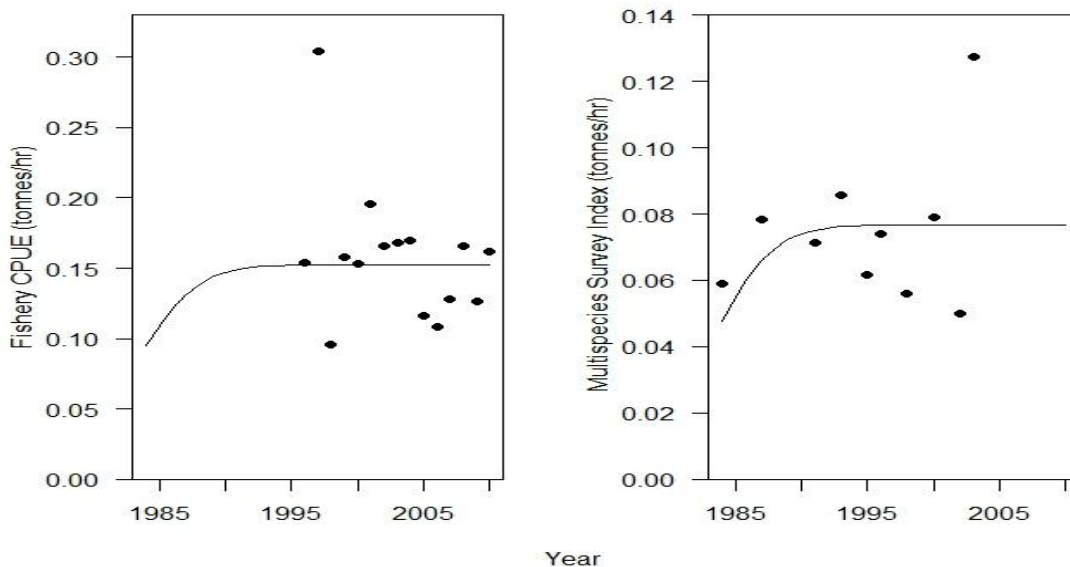
**Figure A2.6.** Posterior distribution of the instantaneous fishing mortality that results in  $MSY$ ,  $F_{MSY}$ , for QCS (solid line) and NHS (dashed line) under a 100% discard mortality rate.



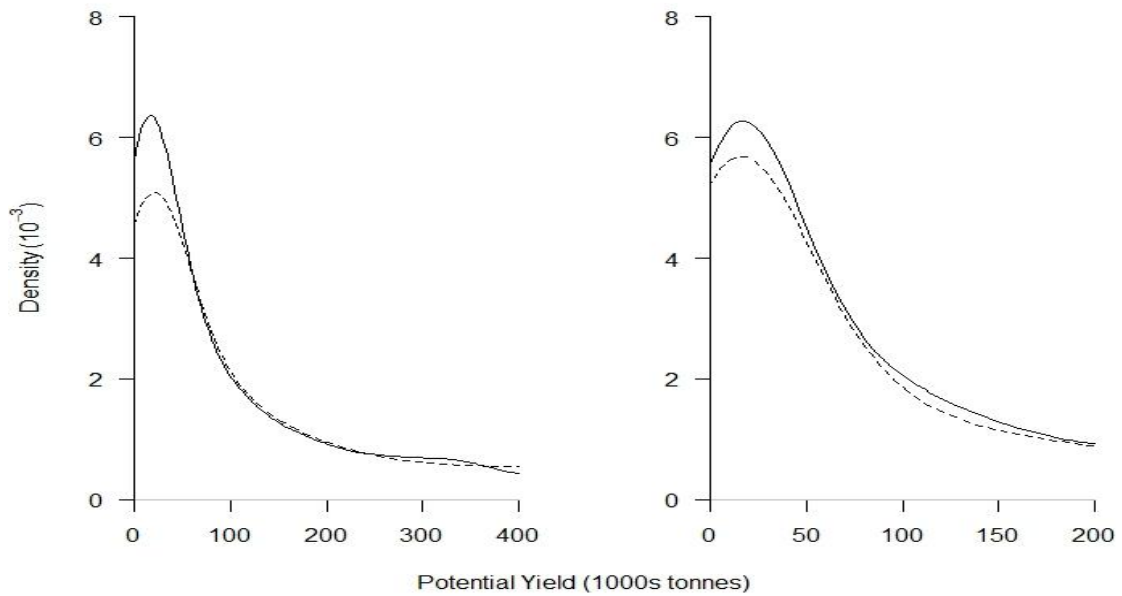
**Figure A2.7.** The log predicted big skate population abundance in QCS (left) from 1996-2010 and NHS (right) from 1984-2010 under a 100% discard mortality rate. The light grey is the 90% quantile, medium grey is the 80% quantile, dark grey is the 50% quantile and the solid black line is the median predicted population biomass.



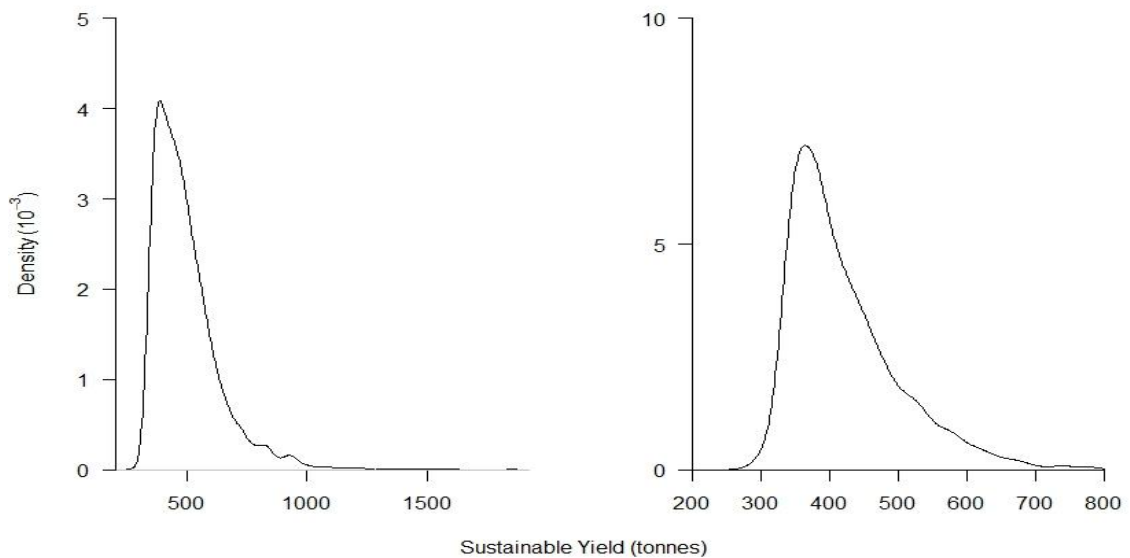
**Figure A2.8.** Observed and predicted indices of abundance for the QCS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters. Fishery CPUE is shown on the left figure, QCS Synoptic Survey in the middle, and QCS Shrimp Survey on the right.



**Figure A2.9.** Observed and predicted indices of abundance for the NHS stock of big skate calculated using the median of the posterior distribution of the three Graham-Schaefer parameters under a 100% discard mortality rate. Fishery CPUE is shown on the left and the Hecate Strait Multispecies Survey on the right.



**Figure A2.10.** Potential yield (solid line) calculated through DCAC compared to MSY (dashed line) estimated from the Graham-Schaefer BDM for QCS (left) and NHS (right).



**Figure A2.11.** Distribution of the sustainable yield calculated using DCAC for the QCS (left) and NHS (right) stocks assuming a 100% discard mortality rate.